



DATA ASSIMILATION IN ENSEMBLE WATER FORECASTING - CHALLENGES AND OPPORTUNITIES

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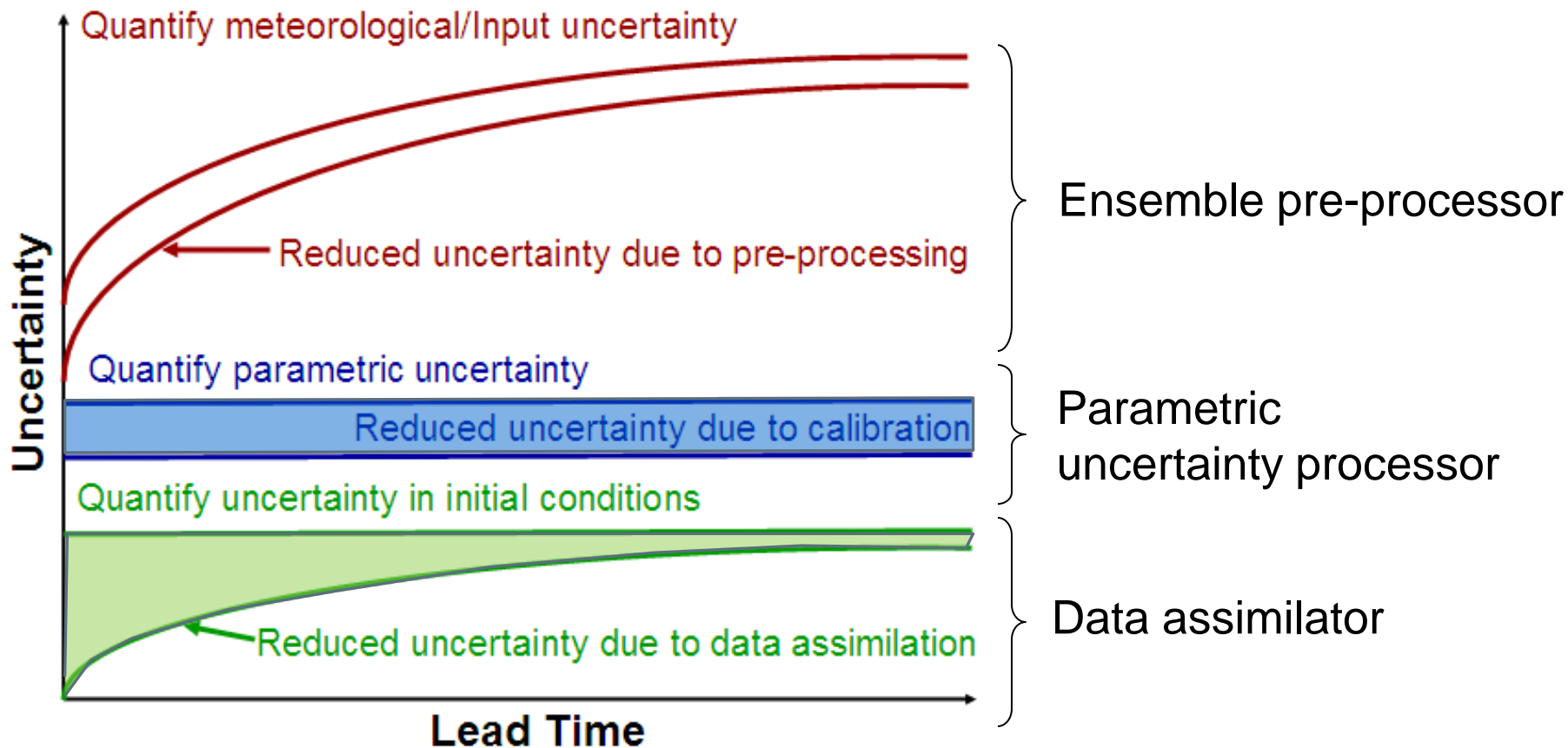
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⁹Retired

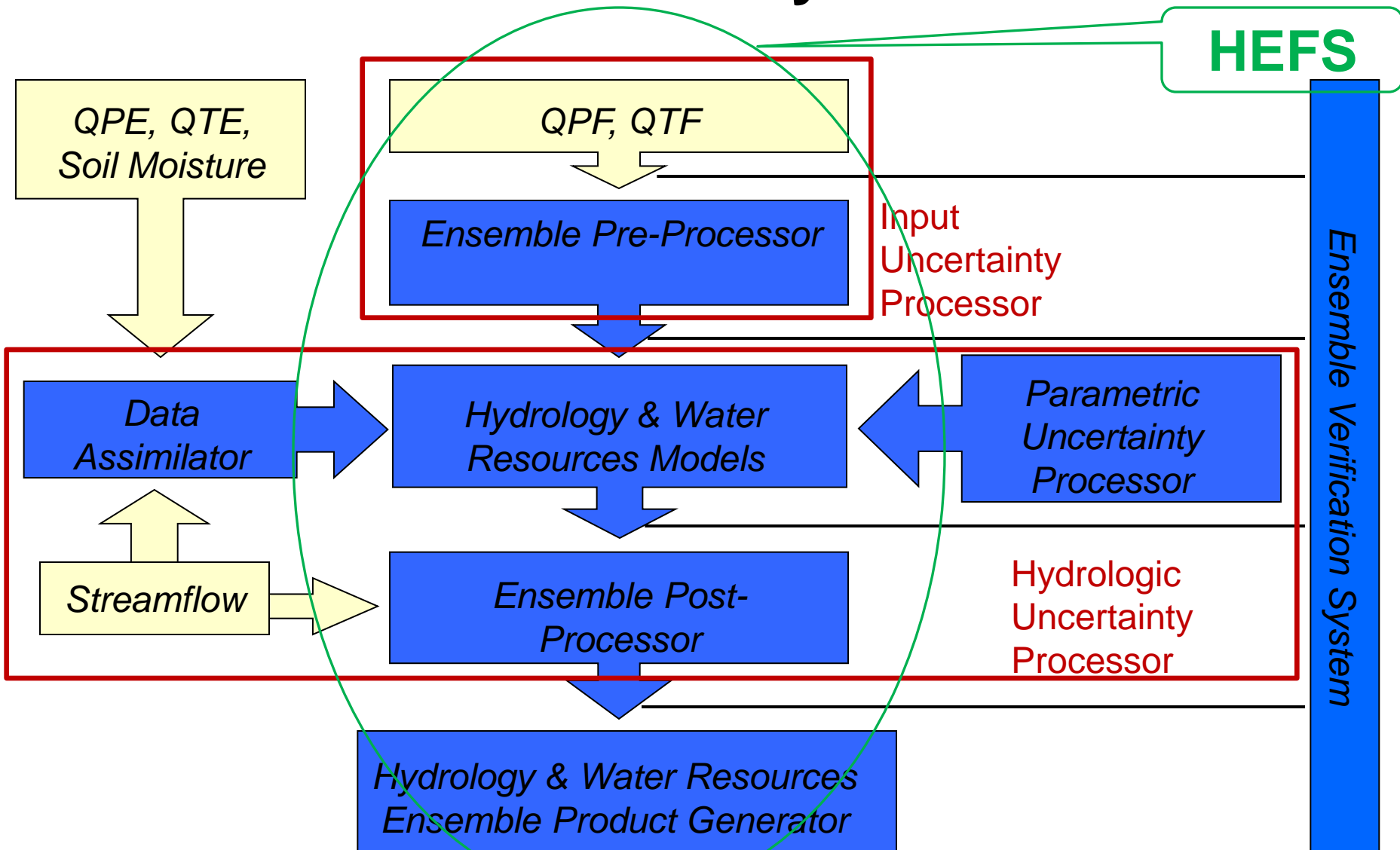
Uncertainties in Hydrologic Forecast



Structural uncertainty } Ensemble post-processor, multimodel
 residual uncertainty } ensemble

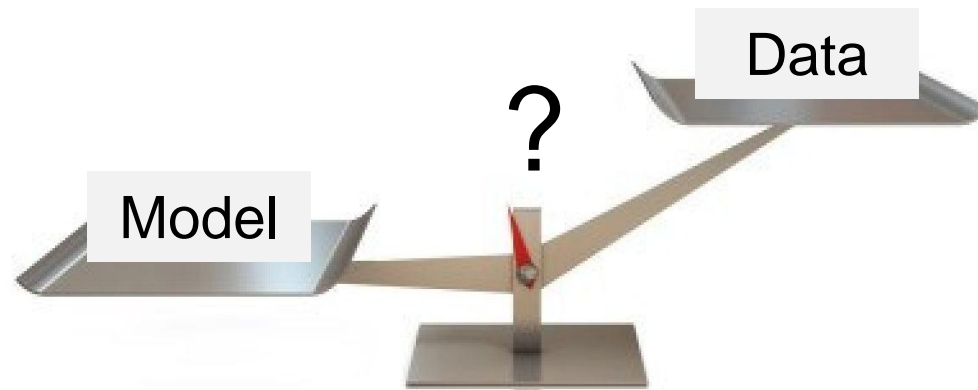
Flow regulations: A large challenge

Elements of Hydrologic Ensemble Prediction System



Data assimilation (DA)

- ***“All models are wrong, but some are useful.” (George E. P. Box)***
- ***“Models are to be used but not to be believed.” (Henry Theil)***
- *Most observations are useful, but some are wrong.*
- *Observations are to be believed but not always to be used.*



History of DA in NWS

- Kitanidis, P. K., and R. L. Bras, 1978. Real time forecasting of river flows. Ralph M. Parsons Lab, Dept of Civil Eng, MIT, TR235.
- Sittner, W. T., and K. M. Krouse, 1979. Improvement of Hydrologic simulation by utilizing observed discharge as an indirect input. NOAA Tech. Memo. NWS HYDRO-38, Silver Spring, MD.
- Carroll, 1979. A procedure to incorporate snow course data in the NWSRFS. Proceedings, Modeling of Snow Cover Runoff, Hanover, NH, 351-358.
- Peck, E. L., E. R. Johnson, K. M. Krouse, T. R. Carroll, and J. C. Schaake, Jr, 1980. Hydrological update techniques used by the US National Weather Service, Proceedings of the Oxford Symposium, IAHS Publ. No. 129.
- Day, G., 1990. A methodology for updating a conceptual snow model with snow measurements, NOAA Technical Report NWS 43, Dept of Commerce, Silver Spring, MD.
- Koren, V. and J. Schaake, 1993. Nile Technical Note #147: Updating Algorithm and Program.
- Georgakakos, K. P. and J. A. Sperflage, 1995. Hydrologic Forecast System – HFS: A user's manual. HRC Tech. Note 1, Hydrologic Research Center, San Diego, CA, 17pp.
- McManamon, A., R. K. Hartman, and R. Hills, 1995. Implementation of the Snow Estimation and Updating System (SEUS) in the Clearwater River Basin, Idaho, Proceedings: 63rd Annual Western Snow Conference, Sparks, NV, 56-65.
- Snow Update System user manual, Version 2.00.02 Updated 2003-09-26, Riverside Technology, Inc.

NWSRFS Operations in use (as of October 2007)

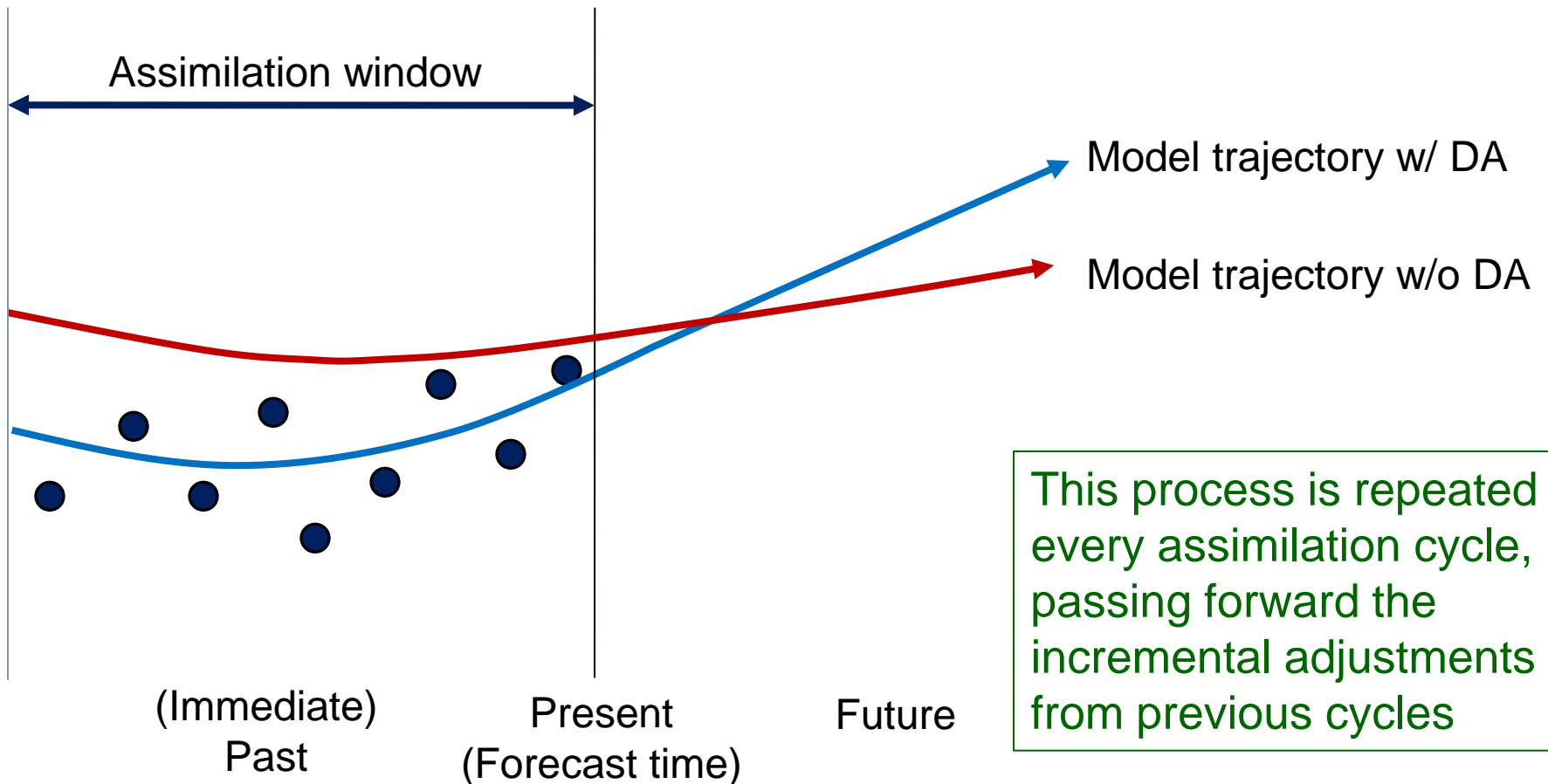
Operation	#RFCs				
ADD/SUB	13	FFG	10	RES-SNGL	11
ADJUST-H	1	FLDWAV	6	RSNWELEV	4
ADJUST-Q	13	GLACIER	1	SAC-SMA	12
ADJUST-T	2	LAG/K	13	SARROUTE	1
API-CONT	1	LAY-COEF	1	RES-J	7
API-HFD	1	LIST-FTW	2	SET-TS	9
API-MKC	1	LOOKUP	11	SNOW-17	10
BASEFLOW	4	LOOKUP3	6	SSARRESV	1
CHANGE-T	13	MEAN-Q	13	SS-SAC	1
CHANLOSS	11	MERGE-TS	12	STAGE-Q	13
CLEAR-TS	13	MULT/DIV	4	STAGEREV	1
CONS_USE	3	MUSKROUT	3	TATUM	2
DELTA-TS	3	NOMSNG	9	TIDEREV	2
DWOPER	3	PLOT-TS	8	UNIT-HG	13
		PLOT-TUL	13	WEIGH-TS	10

Recent prototype DA development in NWS

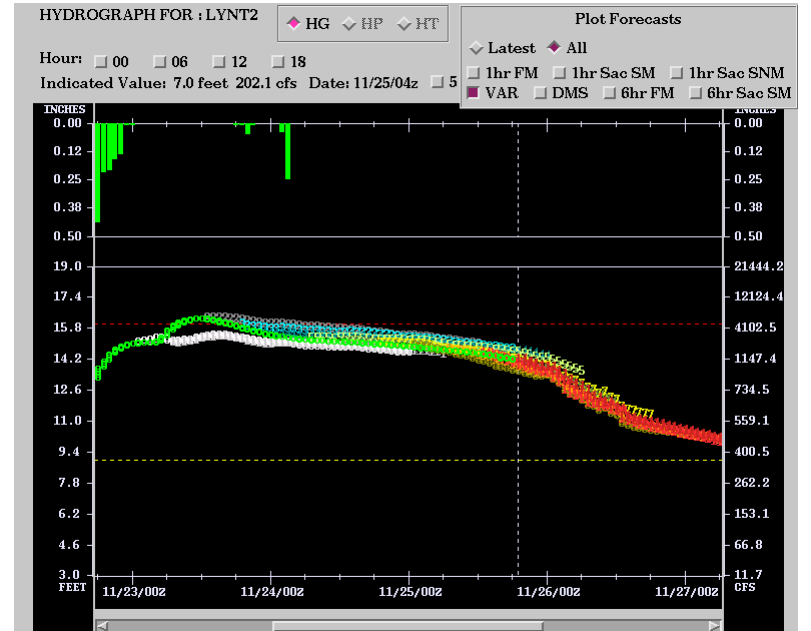
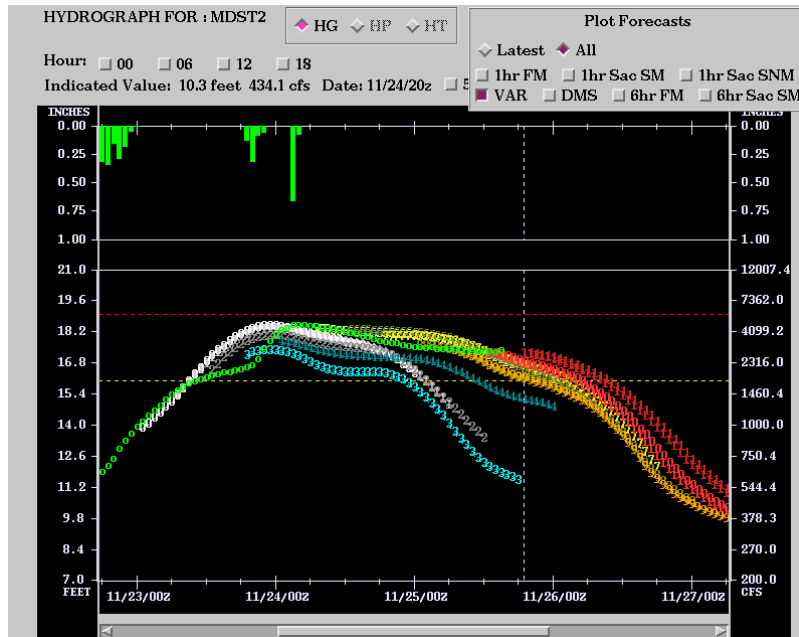
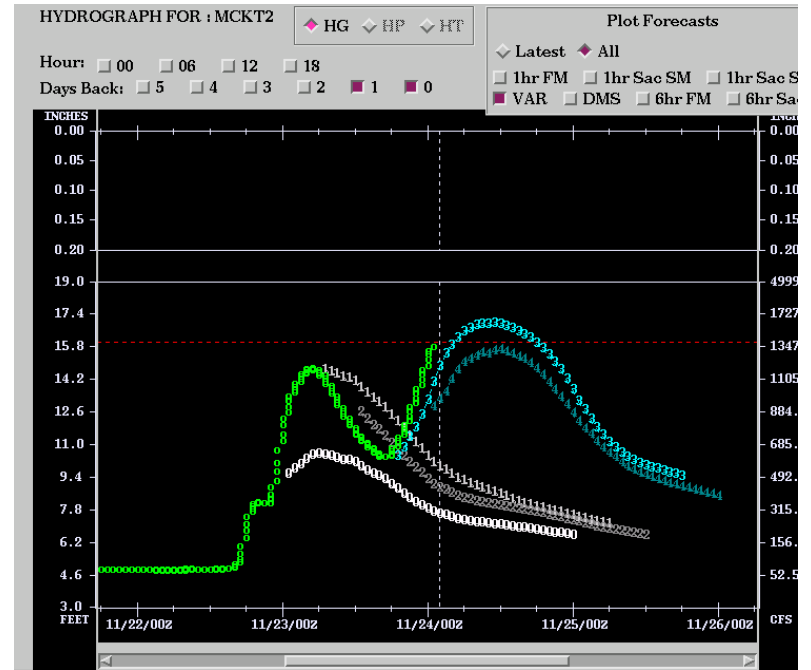
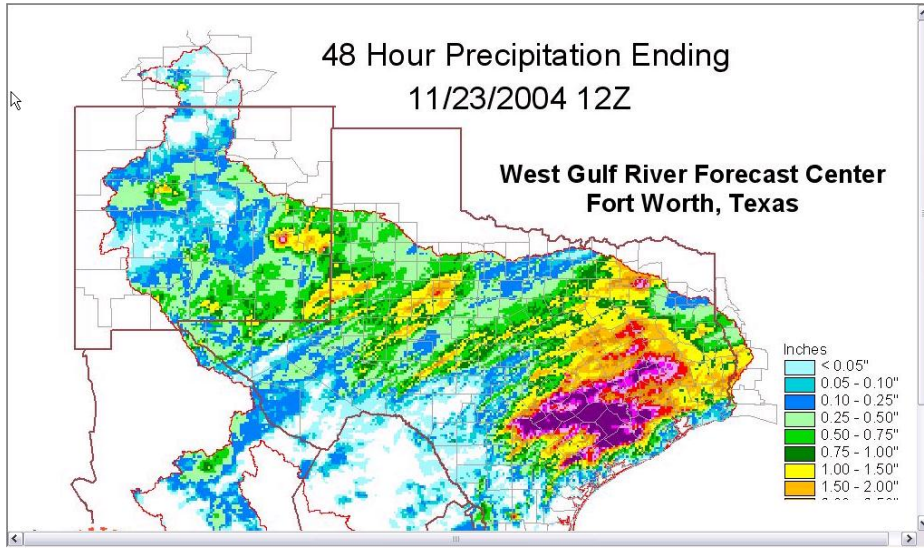
- **State updating for lumped hydrologic model**
 - Sacramento, unit hydrograph
 - 2DVAR
 - Seo et al. (2003, 2008)
 - Implemented in the Site Specific Hydrologic Prediction (SSHP) system
 - Maximum likelihood ensemble filter (MLEF, Zupanski 2005)
- **State updating for distributed hydrologic model**
 - gridded Sacramento, kinematic-wave routing
 - 4DVAR
 - Lee et al. (2011, 2012)
- **Parameter updating for hydrologic routing model**
 - 3-parameter Muskingum routing (O'Donnell 1985)
 - 1DVAR
 - Lee et al. (2011)

Variational assimilation (VAR)

Successive (in time) “batch-by-batch” least-squares curve fitting

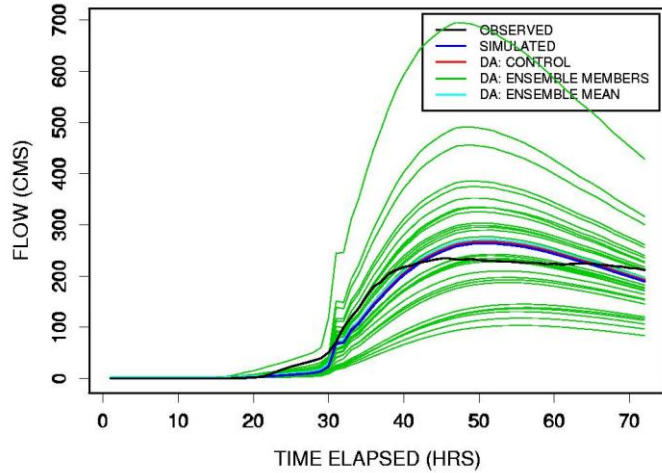


2DVAR-aided forecast as time-lagged ensembles

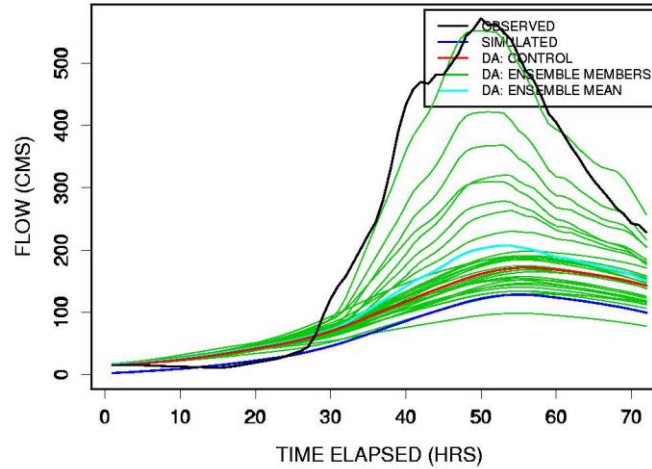


Ensemble filter for lumped SAC-UHG for assimilation of streamflow, precipitation and potential evaporation (PE)

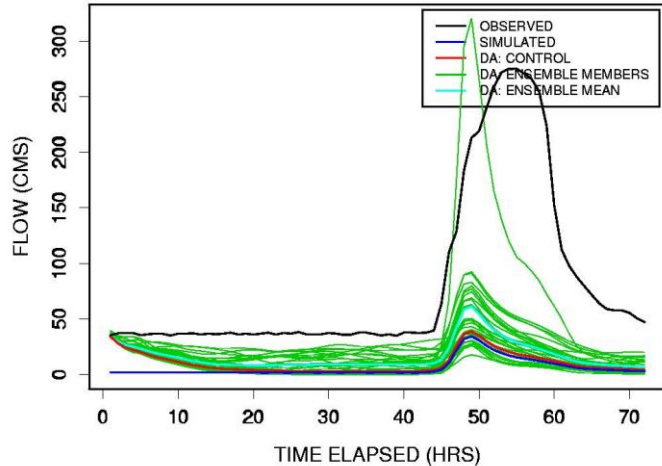
mtpt2 0350 (1998090922)



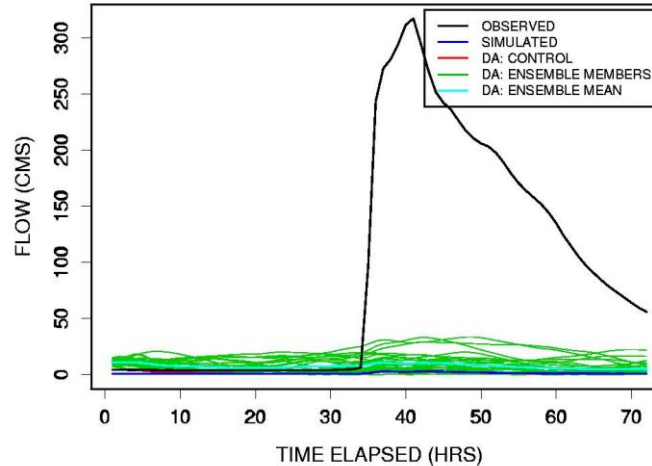
mdst2 0554 (2001060703)



pict2 0661 (1997030809)

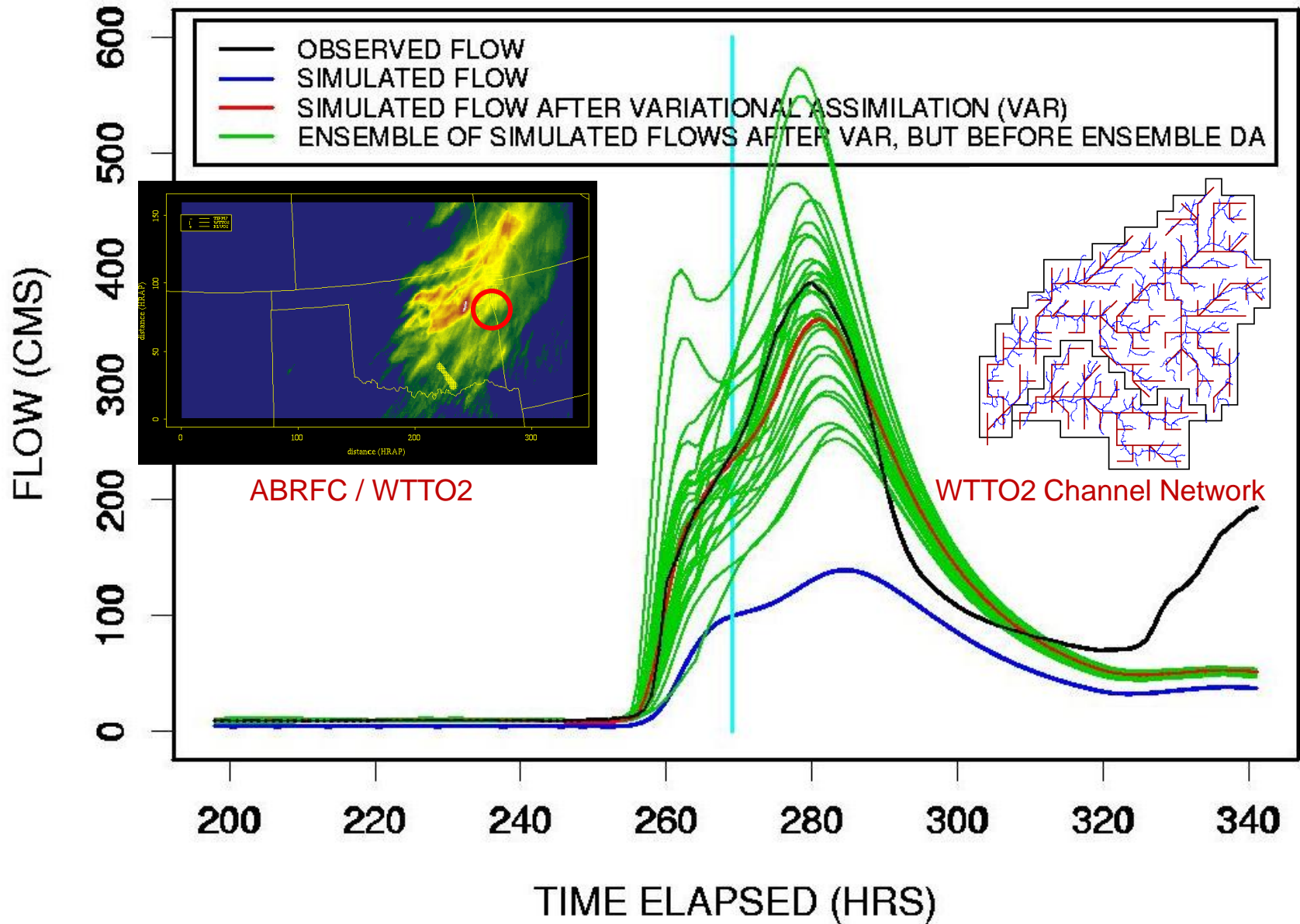


pict2 0183 (1997021106)

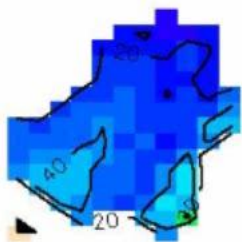


A prototype ensemble filter, a variant of maximum likelihood ensemble filter (Zupanski 2005), for lumped SAC-UHG shows potential (upper plots) and need for improvement (lower plots), including accounting of phase errors and improved error modeling.

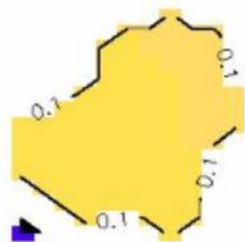
ILLUSTRATION OF DATA ASSIMILATION WITH DISTRIBUTED MODEL



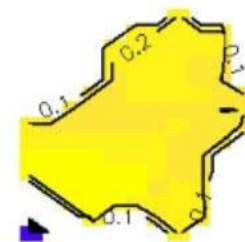
PRECIP (w/o DA)



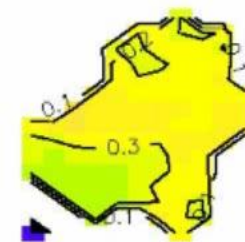
SWC 5cm (w/o DA)



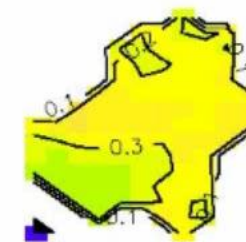
SWC 25cm (w/o DA)



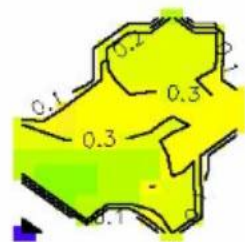
SWC 60cm (w/o DA)



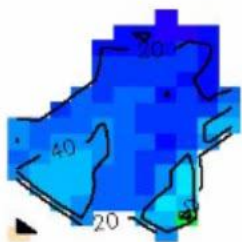
SWC 75cm (w/o DA)



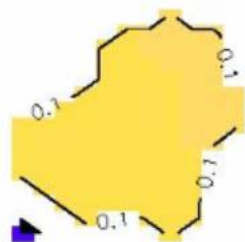
SWC 1m (w/o DA)



PRECIP (w/ DA)



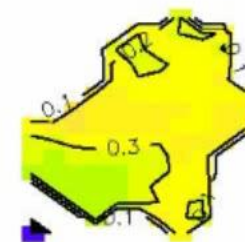
SWC 5cm (w/ DA)



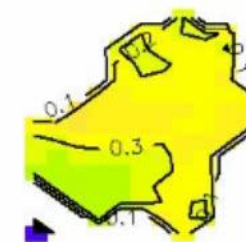
SWC 25cm (w/ DA)



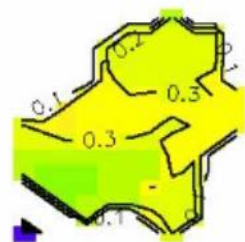
SWC 50cm (w/ DA)



SWC 75cm (w/ DA)



SWC 1m (w/ DA)



HSLOPE (w/o DA)



CHANNEL (w/o DA)



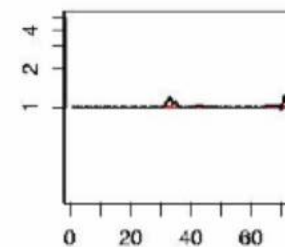
CHANNEL (w/o DA)



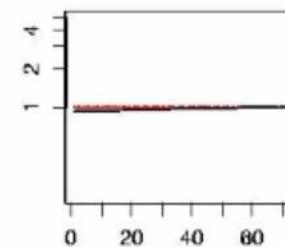
CHANNEL (w/o DA)



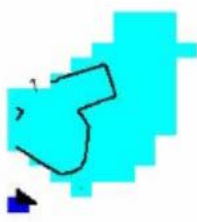
BIAS IN PRECIP



BIAS IN PE



HSLOPE (w/ DA)



CHANNEL (w/ DA)



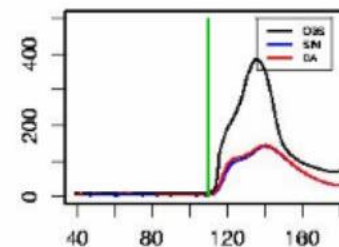
CHANNEL (w/ DA)



CHANNEL (w/ DA)

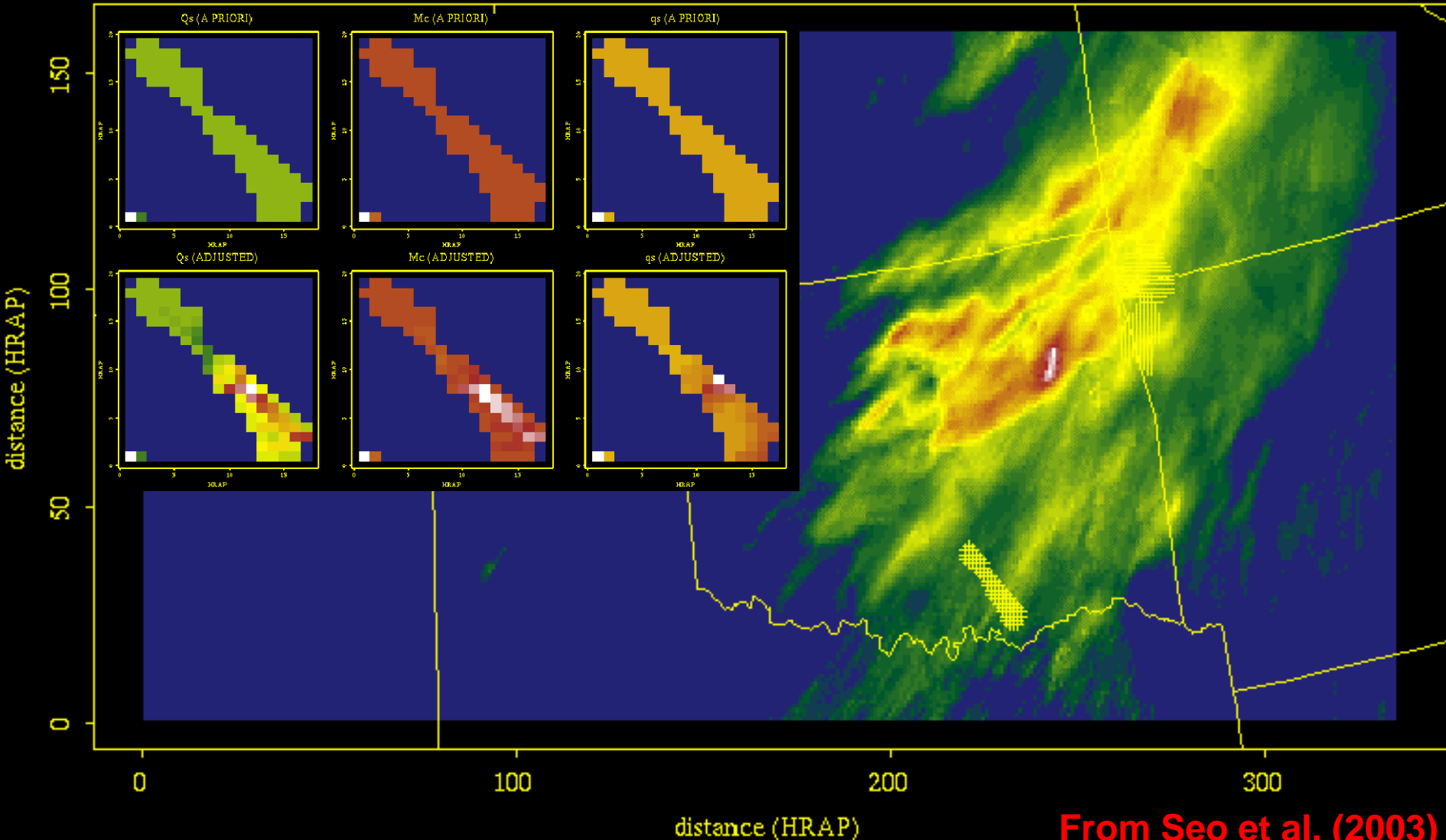


OUTLET STREAMFLOW (CMS)



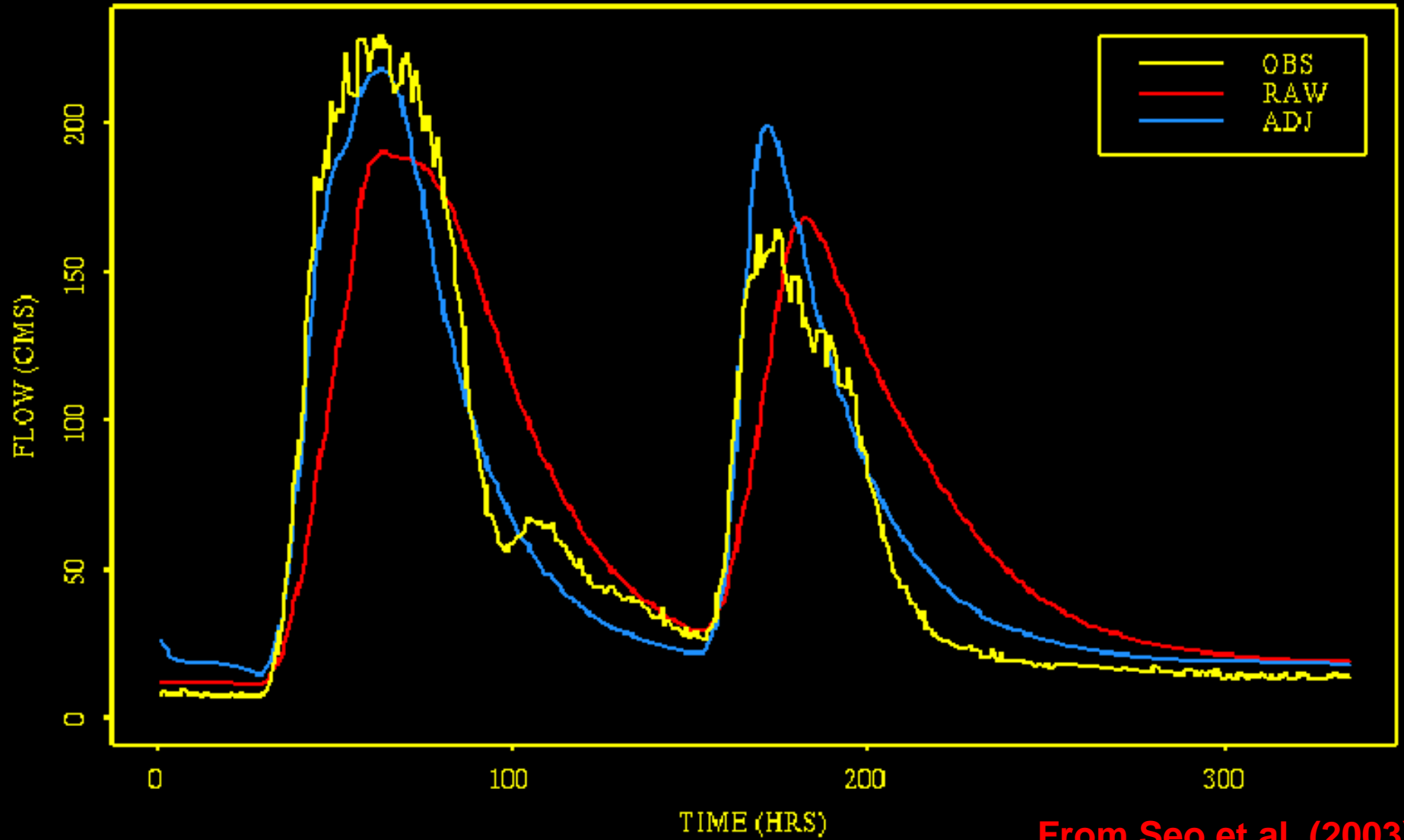
WTTO2 HR 00110
1993111400

Parameter estimation/optimization of distributed hydrologic routing model



From Seo et al. (2003)

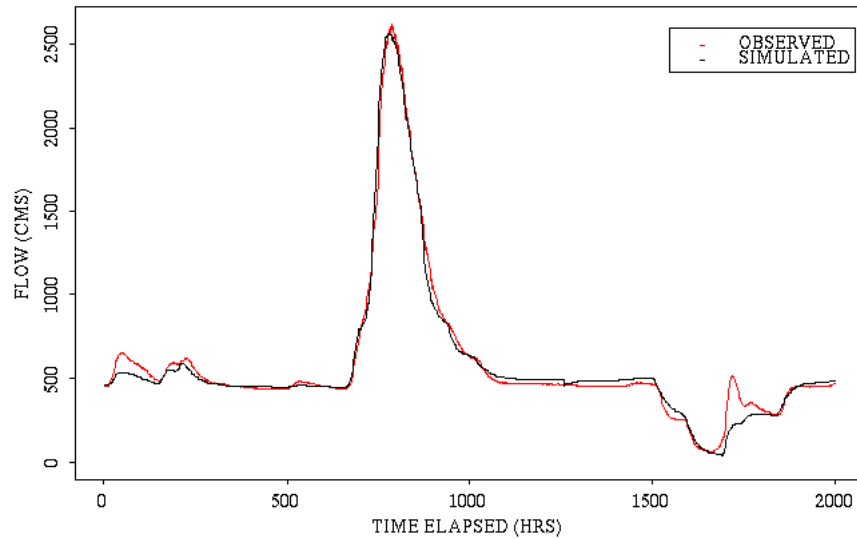
BLUO2 – Nov 11 ~ Dec 6, 1996



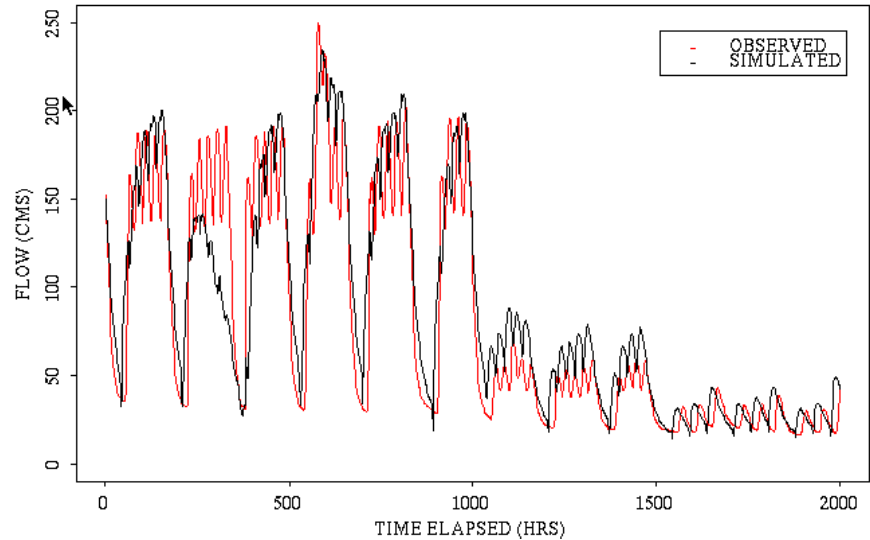
From Seo et al. (2003)

Toward ensemble DA for hydrologic routing – parameter estimation for variable 3-parameter Muskingum routing (O’Donnell 1985)

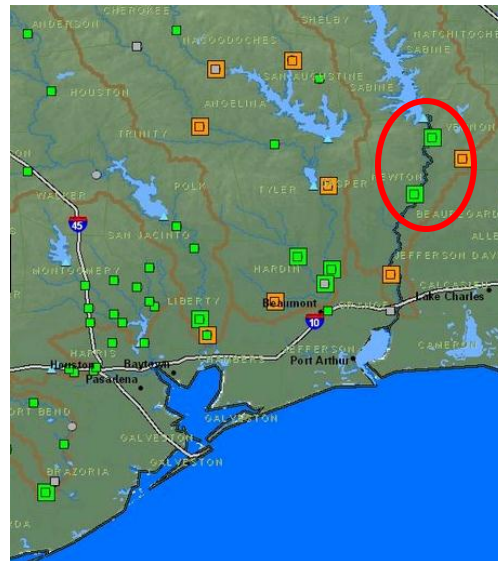
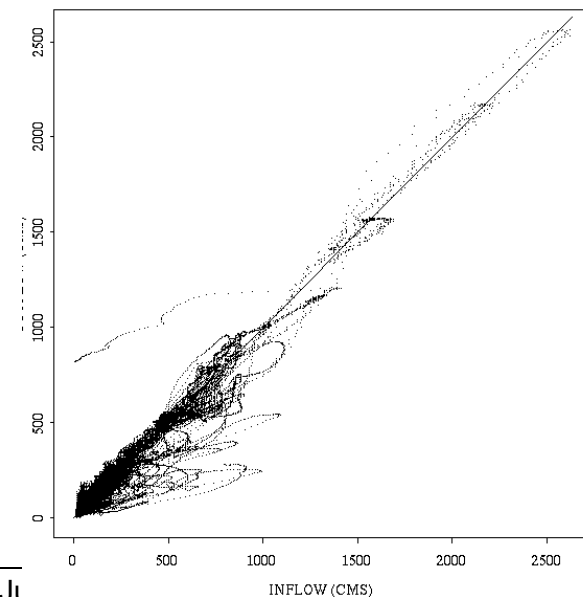
BRVT2_BWRT2



BRVT2_BWRT2



BRVT2_BWRT2 (corr=0.97)



Many NWS forecast points require routing of upstream forecasts to the downstream locations. Very often, such routing is subject to flow regulations (upper-right) and sources and sinks that are not very well accounted for (lower-left). Real-time DA can help improve forecast accuracy and quantify uncertainty.

2DVAR - Lessons learned

- Use the same, operational models (soil moisture accounting, snow, routing, etc.)
 - Model physics and parameters must be the same and completely transferable
- Allow forecaster control
 - To reflect any prior or additional information that the forecaster may have
 - Restart (warm or cold) may be necessary if the model deviates from the real world
- Provide, and effectively present, model-dynamical information that explains the DA results
 - Displays of with- and without-DA results over multiple time periods for pattern identification
- Clearly demonstrate the value of DA through objective comparative verification
 - In the context of the end-to-end forecast process
 - Relative to the current operational practice
- Training

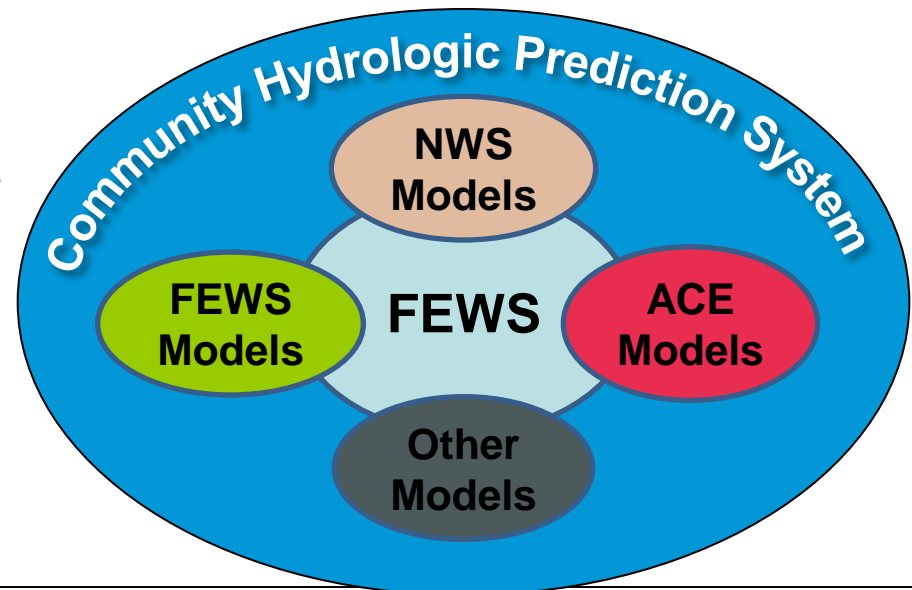
Community Hydrologic Prediction System (CHPS)

Flexible, open modeling architecture *linking* program elements

- Modular software to enhance collaboration and accelerate R2O
- Extension of the Flood Early Warning System (FEWS) architecture:
 - Incorporates NWS models with models from FEWS, U.S. Army Corps of Engineers (ACE), and academia

Implementation Status:

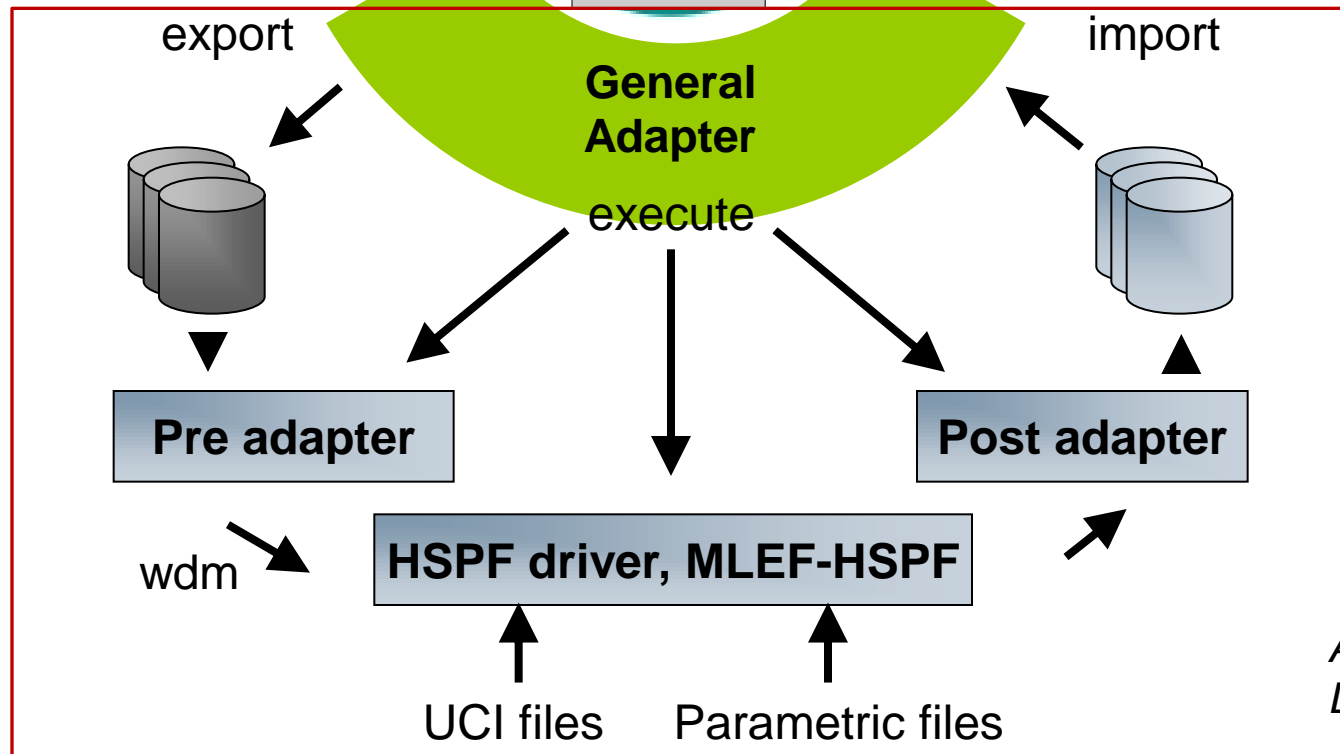
- ✓ AWIPS-II compatible prototype hardware and software for all RFCs
- ✓ Conducting parallel operations at 4 RFCs, remaining by early 2011
- ✓ Retire legacy system in early 2012



From Carter (2010)

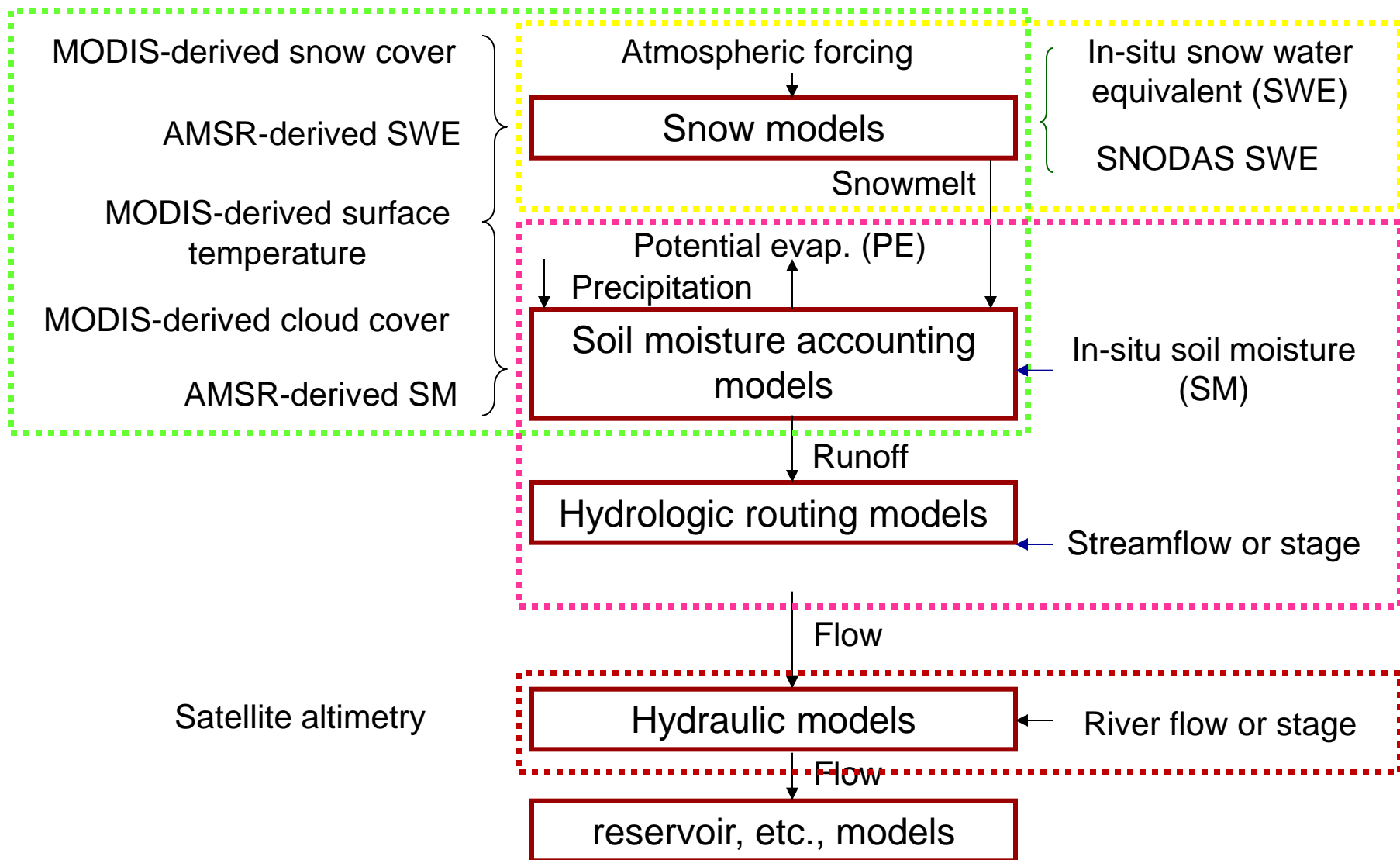
Implementation of MLEF-HSPF in FEWS-NIER as a new model

<http://www.opendata.org/joomla/index.php>



*Adapted from
Deltares (2012)*

Operational hydrologic data assimilation - Strategy

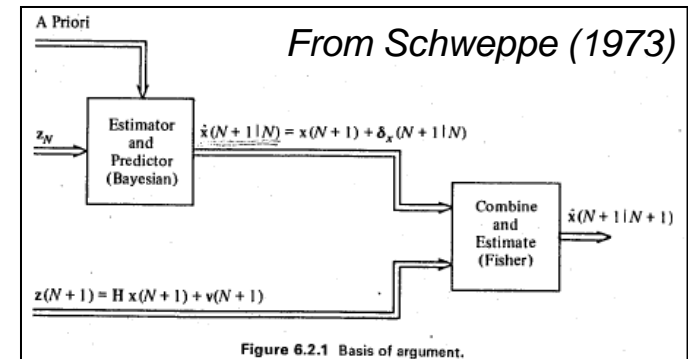


Adapted from OHD Strategic Science Plan 2010

DA strategy for operational hydrologic forecasting

- Decompose $Z = f(X, V)$
- To illustrate, decompose:

$$\begin{bmatrix} Z_1 \\ Z_2 \\ \cdot \\ \cdot \\ Z_n \end{bmatrix} = \begin{bmatrix} H_{11} & H_{12} & \cdot & \cdot & H_{1m} \\ H_{21} & H_{22} & \cdot & \cdot & H_{2m} \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ H_{n1} & H_{n2} & \cdot & \cdot & H_{nm} \end{bmatrix} \begin{bmatrix} X_1 \\ X_2 \\ \cdot \\ \cdot \\ X_m \end{bmatrix} + \begin{bmatrix} V_1 \\ V_2 \\ \cdot \\ \cdot \\ V_n \end{bmatrix}$$



into smaller ones such that:

- the suboptimal solutions from the decomposed problems are close to the optimal solution for the full-blown problem
- the resulting DA process is forecaster-controllable

Questions



- Uncertain error statistics
 - Nonlinear, heteroscedastic, flow- and scale-dependent
- Underdetermined systems
 - Paucity of observations
 - Rank deficiency a large issue
- Nonlinear observations
 - Streamflow for soil moisture
- Minimization criteria
 - Need for DA is for out-of-the-ordinary/extreme events
 - Climate change, urbanization

The “PQR” problem (from the 1st HEPEX DA Workshop in Delft, Nov, 2010)

$$\hat{\mathbf{x}}(N+1|N+1) = \Sigma(N+1|N+1) \times \{ \mathbf{H}'(N+1) \mathbf{R}^{-1}(N+1) \mathbf{z}(N+1) + \Sigma^{-1}(N+1|N) \Phi(N) \hat{\mathbf{x}}(N|N) \}$$

$$\Sigma(N+1|N) = \Phi(N) \Sigma(N|N) \Phi'(N) + \mathbf{G}(N) \mathbf{Q}(N) \mathbf{G}'(N)$$

$$\Sigma(N+1|N+1) = [\mathbf{H}'(N+1) \mathbf{R}^{-1}(N+1) \mathbf{H}(N+1) + \Sigma^{-1}(N+1|N)]^{-1}$$

$$\Sigma(0|0) = \Psi$$

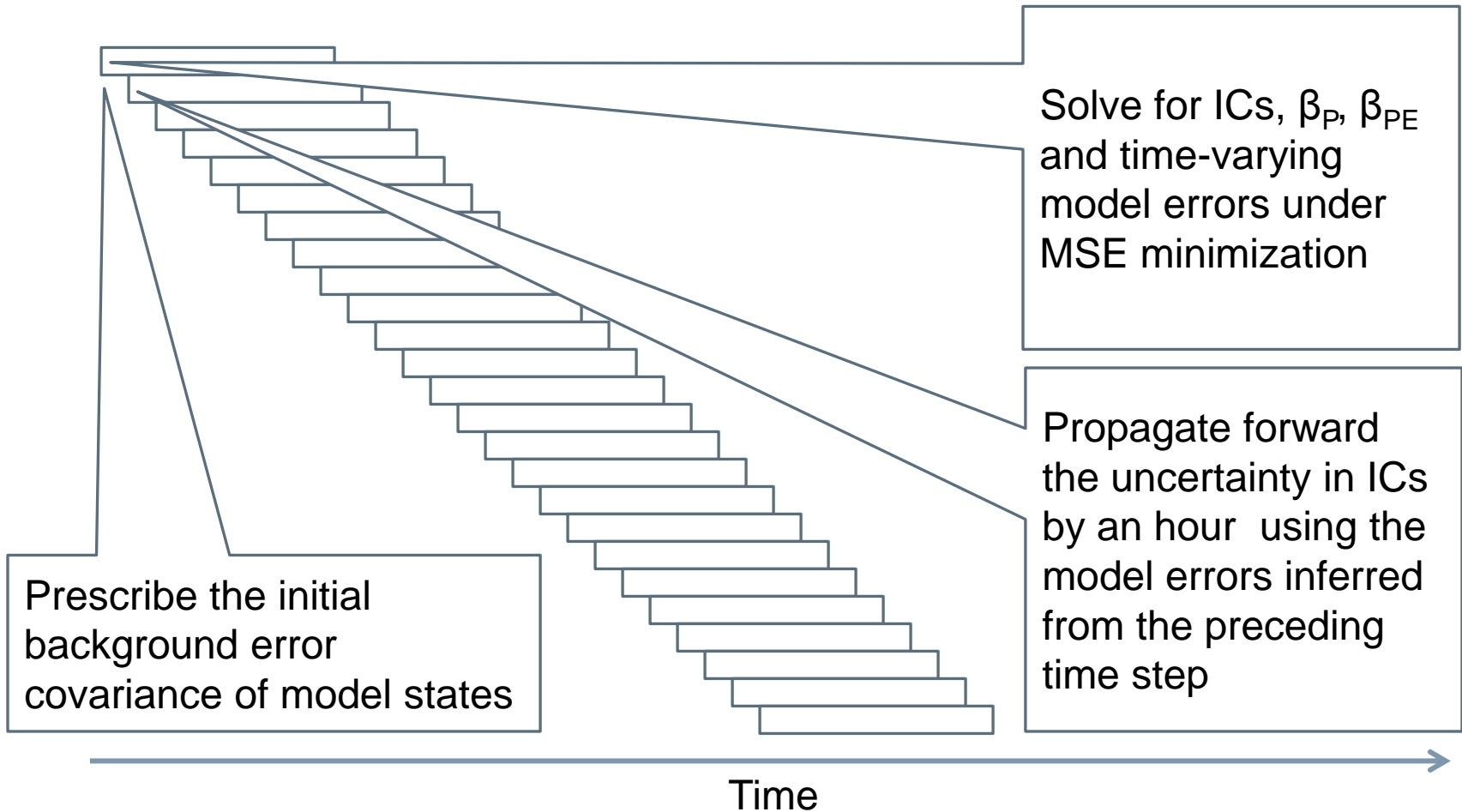
$$\hat{\mathbf{x}}(0|0) = \mathbf{0}$$

From Schweppe (1973)

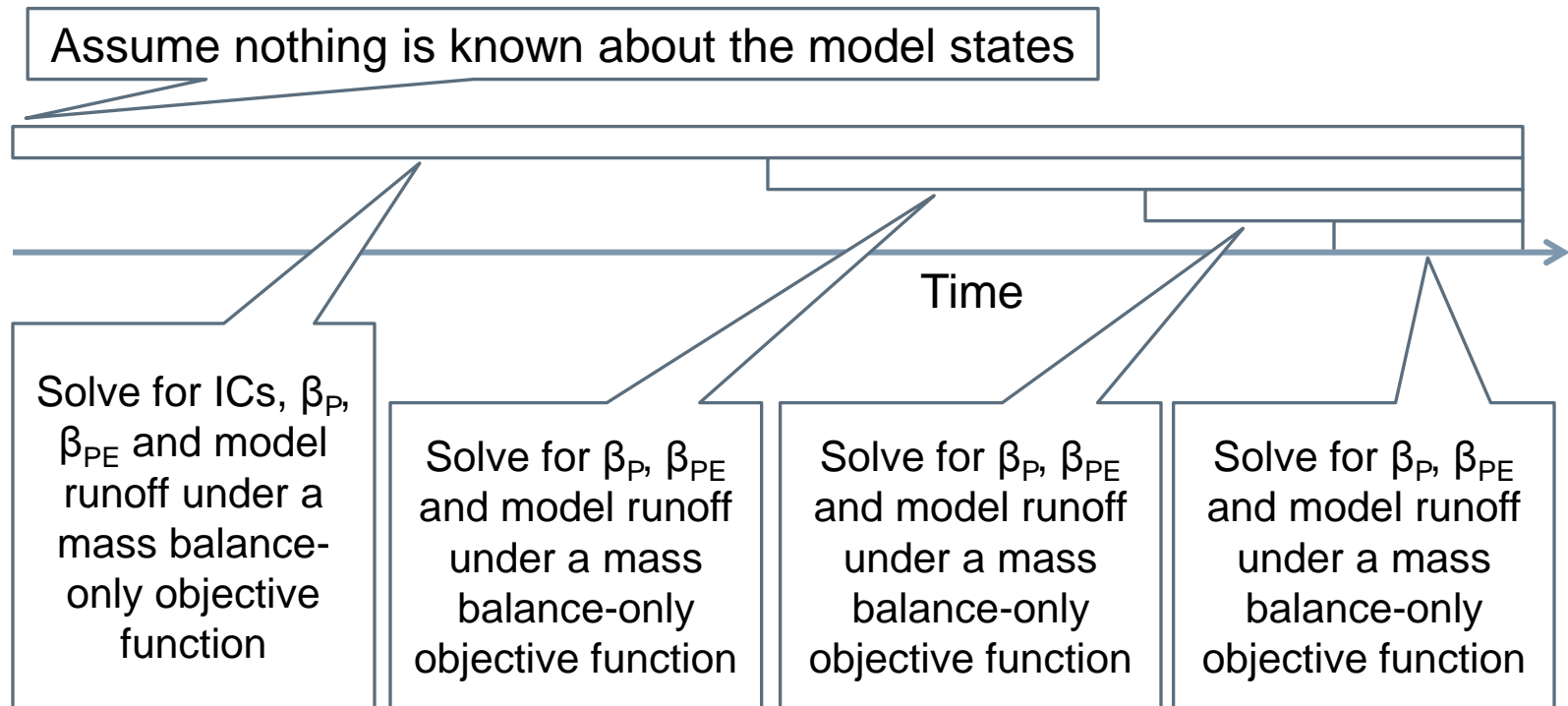
Proposed approach

- Multi-Scale Bias Correction (MSBC)
 - The hydrologic processes (and hence model errors) are multiscale in nature due to different residence times at work.
 - Due to paucity of hydrologic observations, the DA problems are likely to be underdetermined.
- Adaptive Error Modeling (AEM)
 - Rather than modeling process-specific errors in soil moisture and routing dynamics, model the aggregate errors in runoff simulation based on observed streamflow for
 - parsimony
 - adaptive accounting of heteroscedasticity and timing errors.

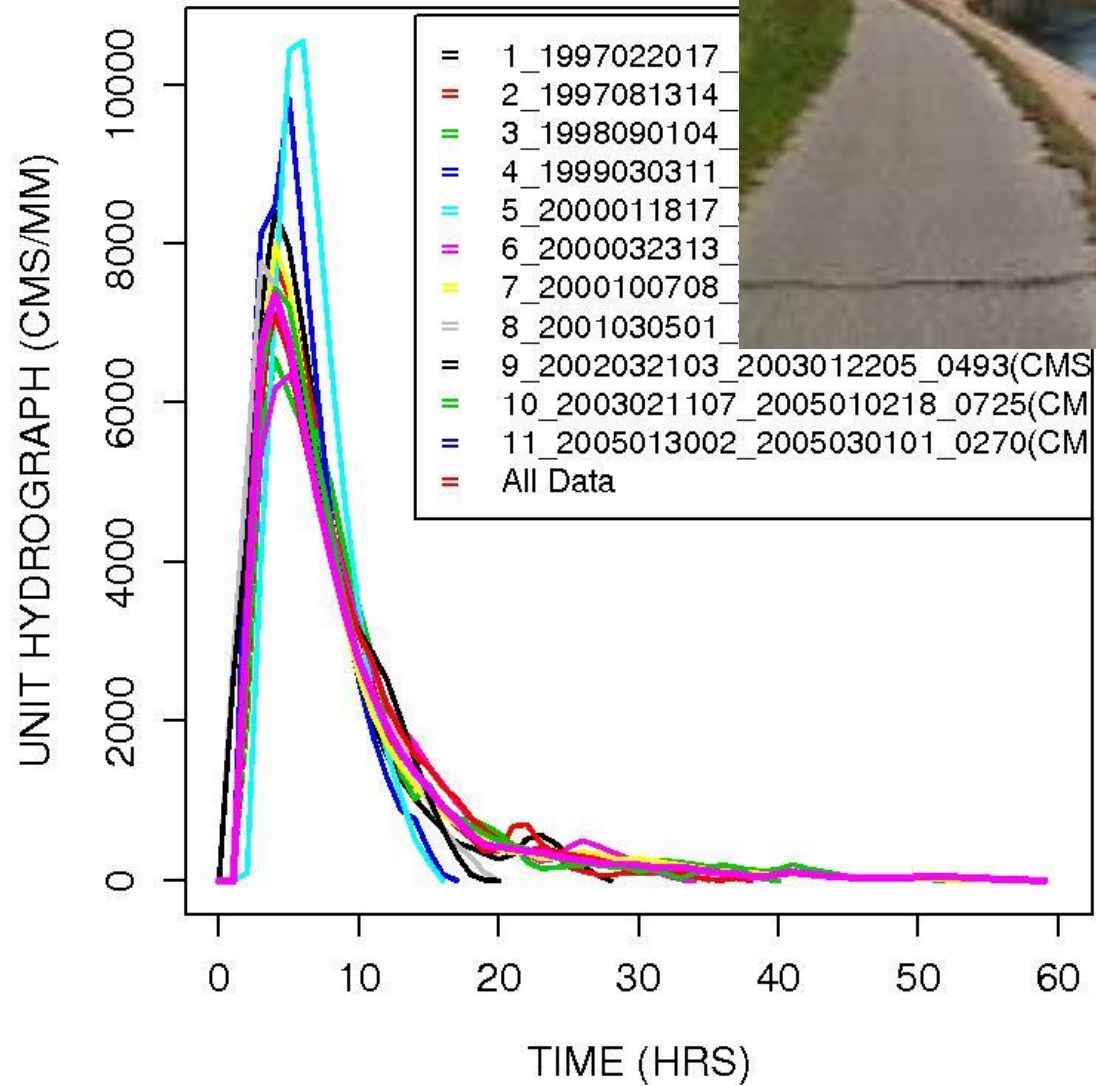
2DVAR with forward propagation of IC



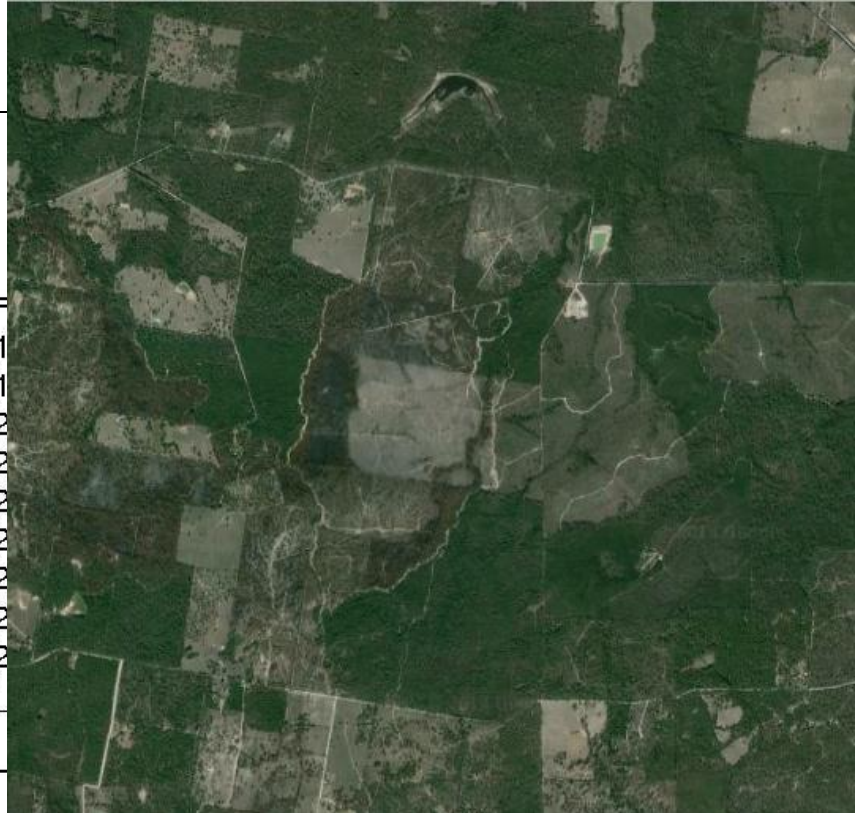
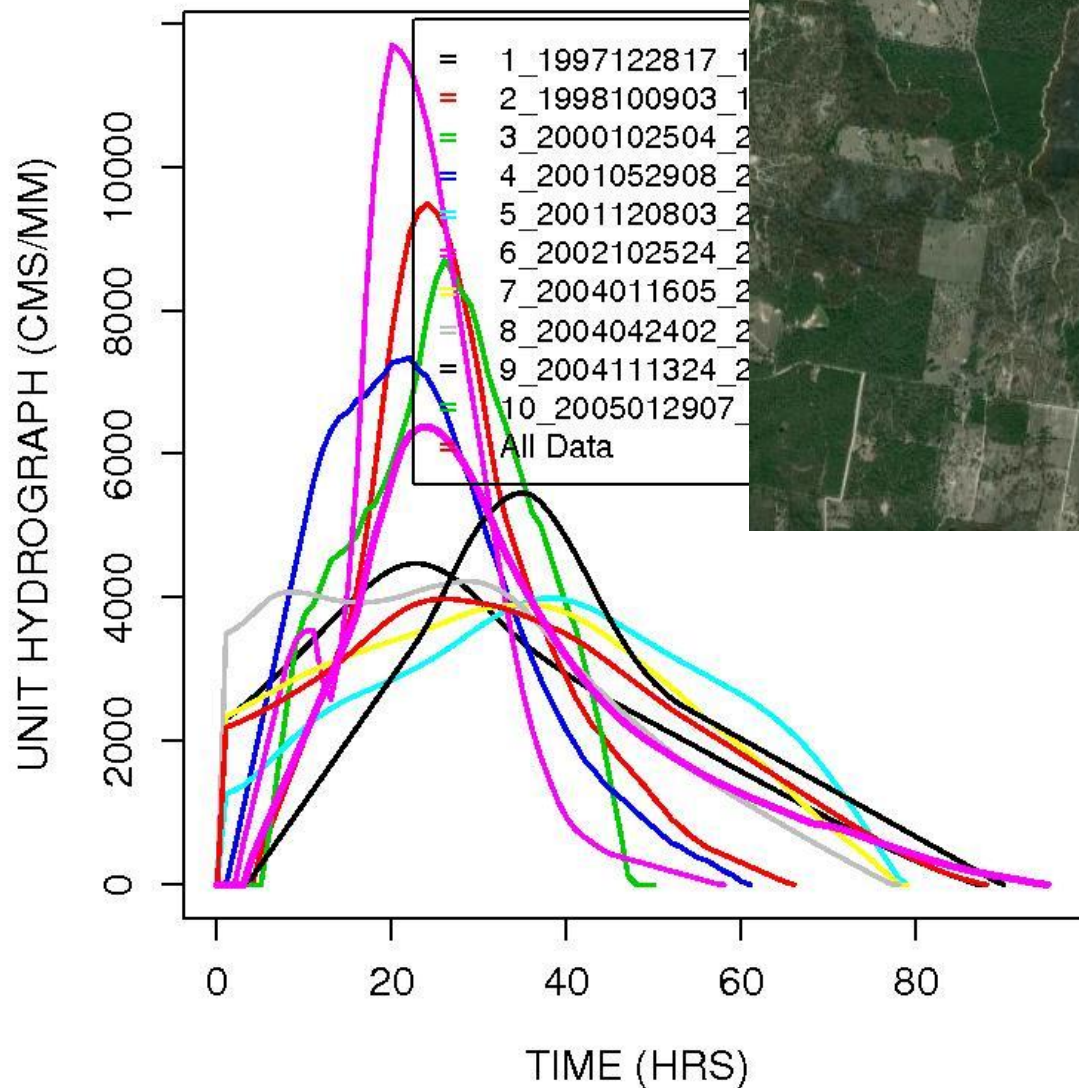
Multi-Scale Bias Correction (MSBC)



hbmt2

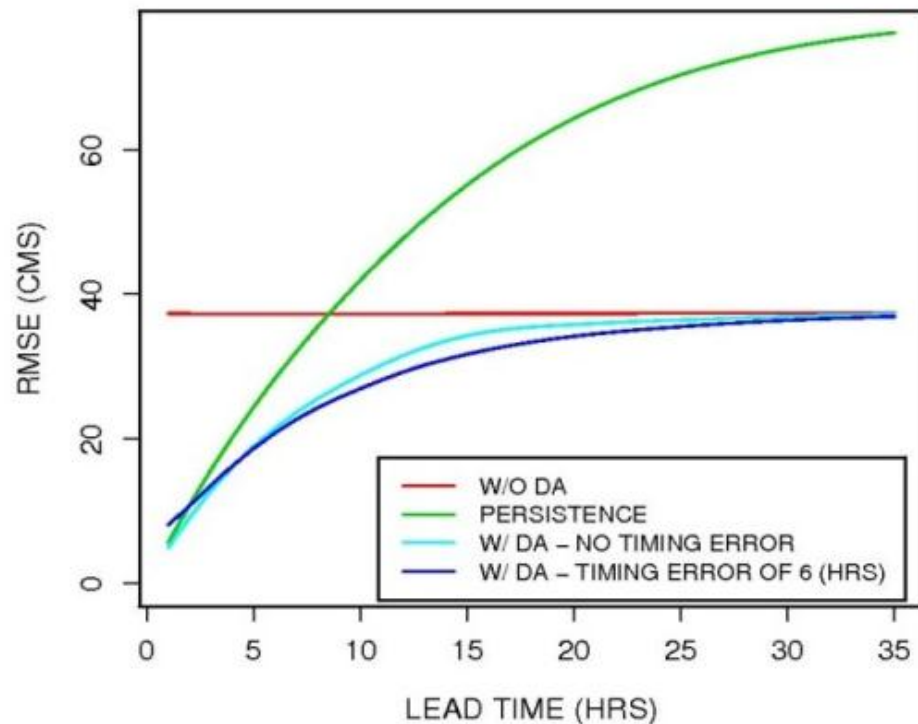


MDST2



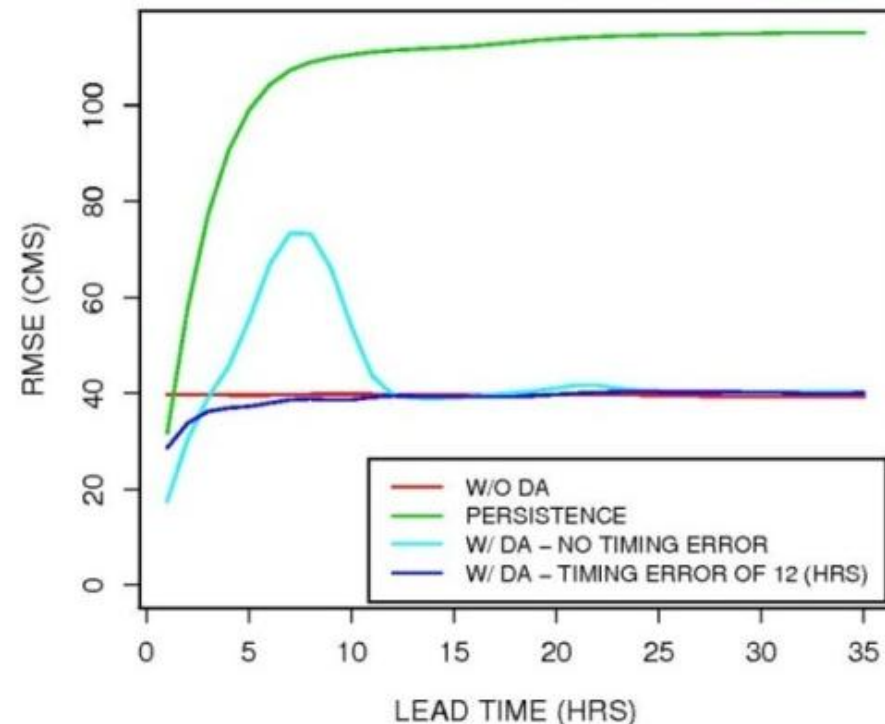
Effect of timing errors in updating of soil water states

MCKT2



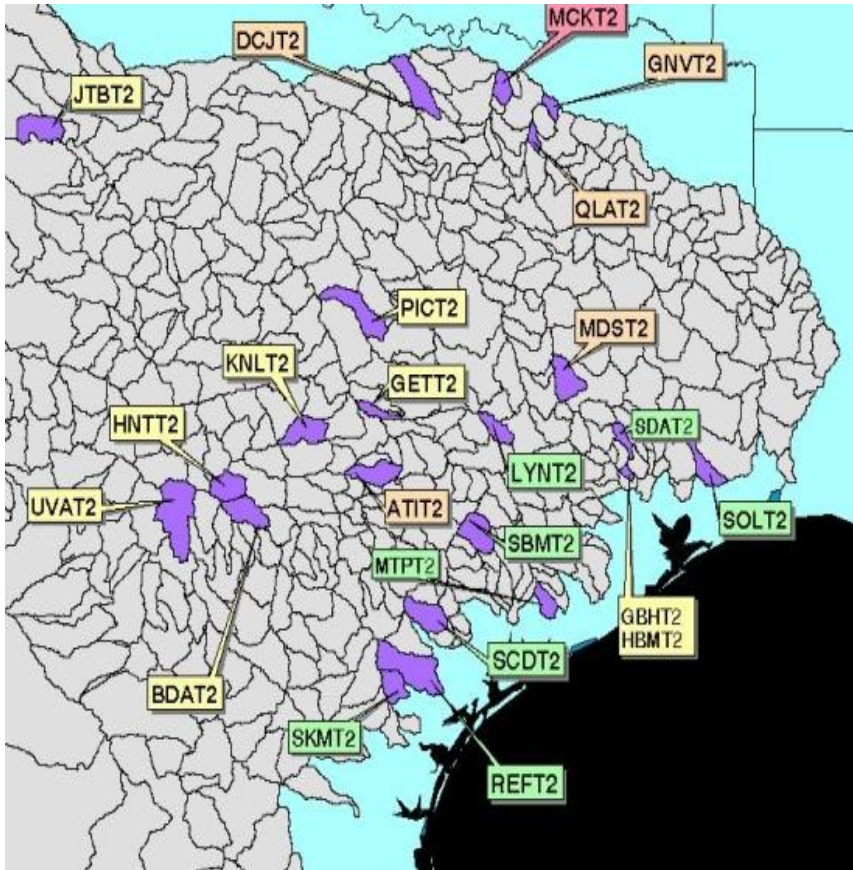
$T_p=13$ (hrs)

GETT2



$T_p=10$ (hrs)

MSBC vs. 2DVAR



2DVAR better

3 basins

MSBC better

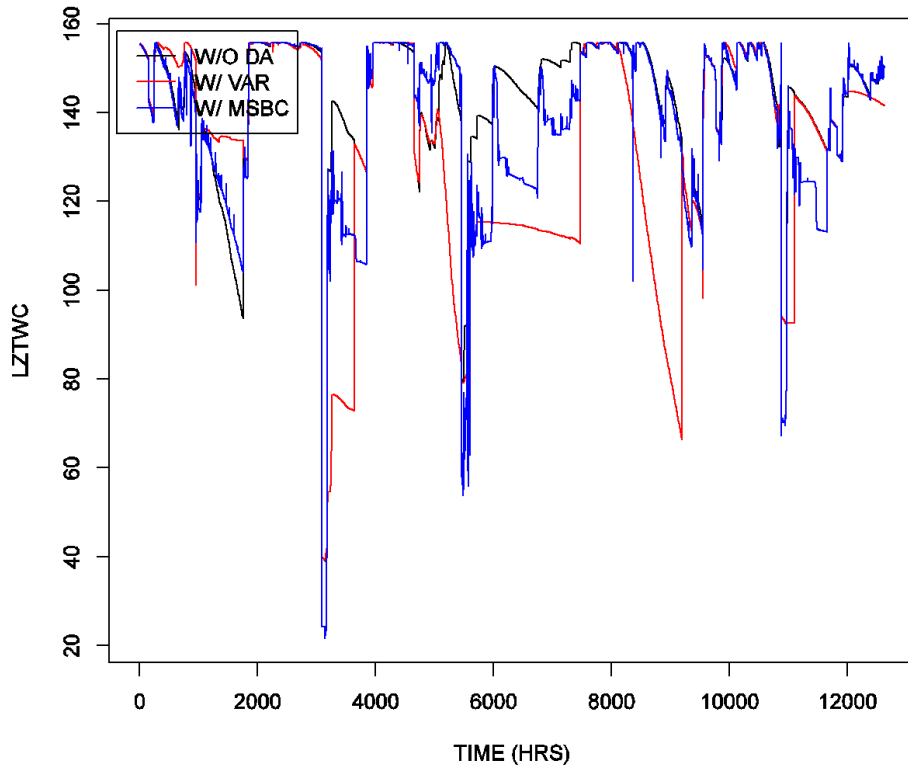
10 basins

Comparable

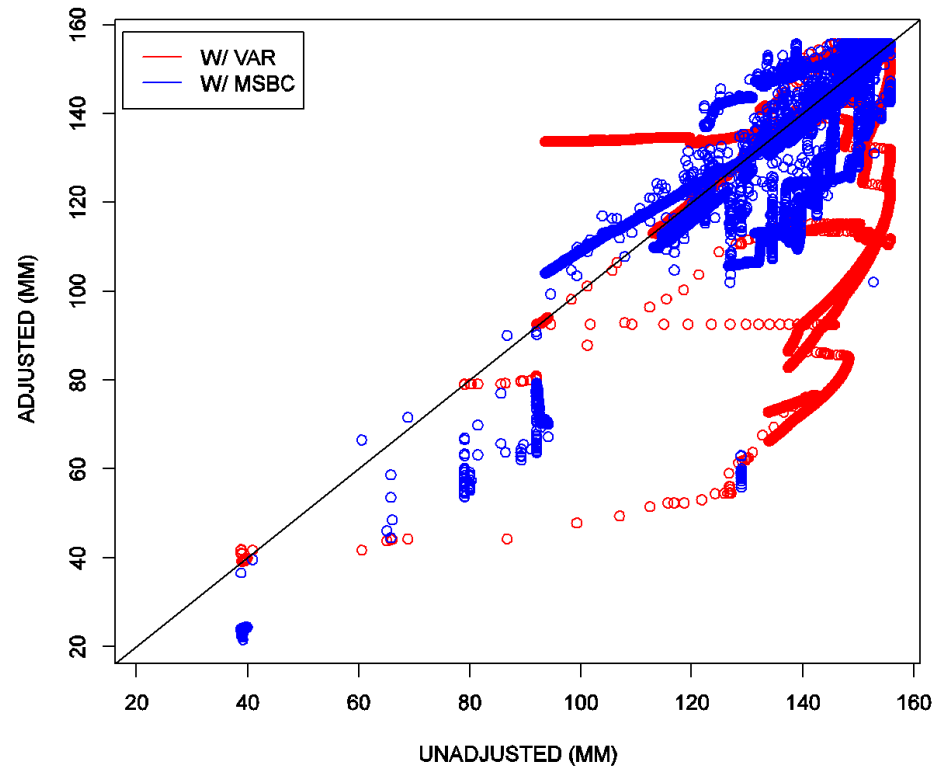
10 basins

MSBC-updated model states stay much closer to the base (i.e. un-updated) model states

LZTWC for GNV2_10_00

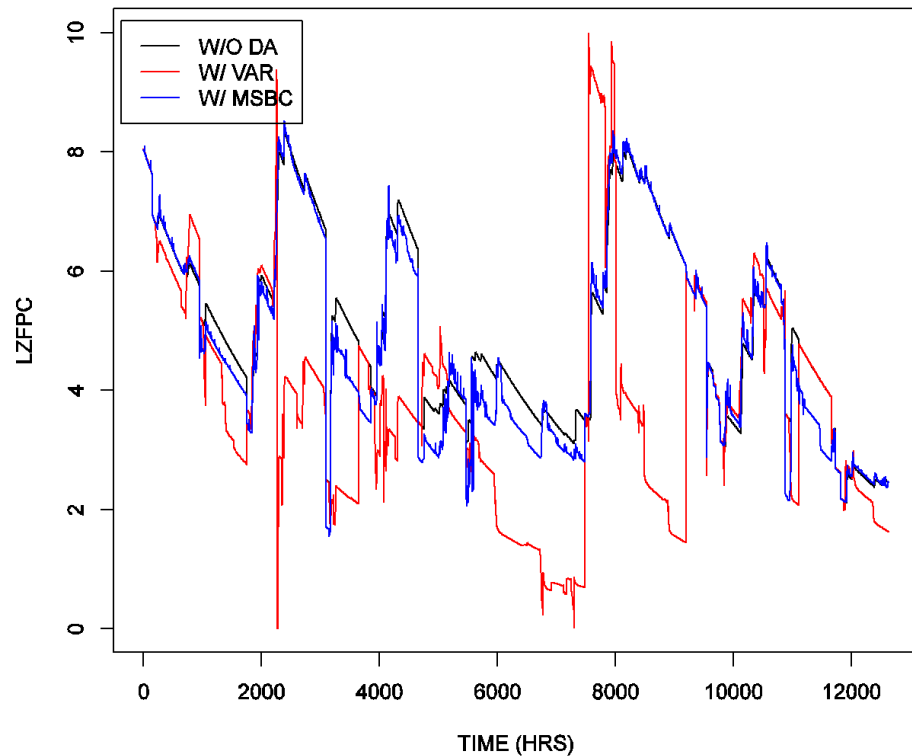


LZTWC for GNV2_10_00

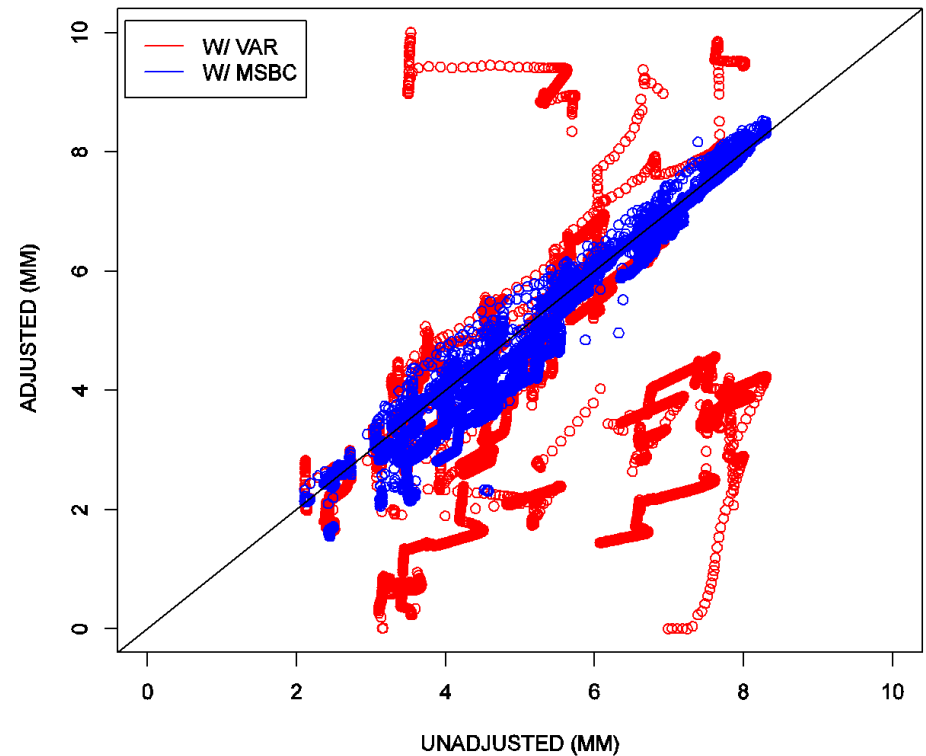


MSBC-updated model states stay much closer to the base model states (cont.)

LZFPC for GNV2_10_00



LZFPC for GNV2_10_00



Dealing with nonlinear observations

$$\mathbf{x}(n+1) = \mathbf{\Phi}(n)\mathbf{x}(n) + \mathbf{G}(n)\mathbf{w}(n)$$

$$\mathbf{z}(n) = \mathbf{H}(n)\mathbf{x}(n) + \mathbf{v}(n), \quad n = 1, \dots$$

$\mathbf{x}(n)$ state, a K_1 vector

$\mathbf{z}(n)$ observation, a K_2 vector

$\mathbf{v}(n)$ white observation uncertainty, a K_2 vector

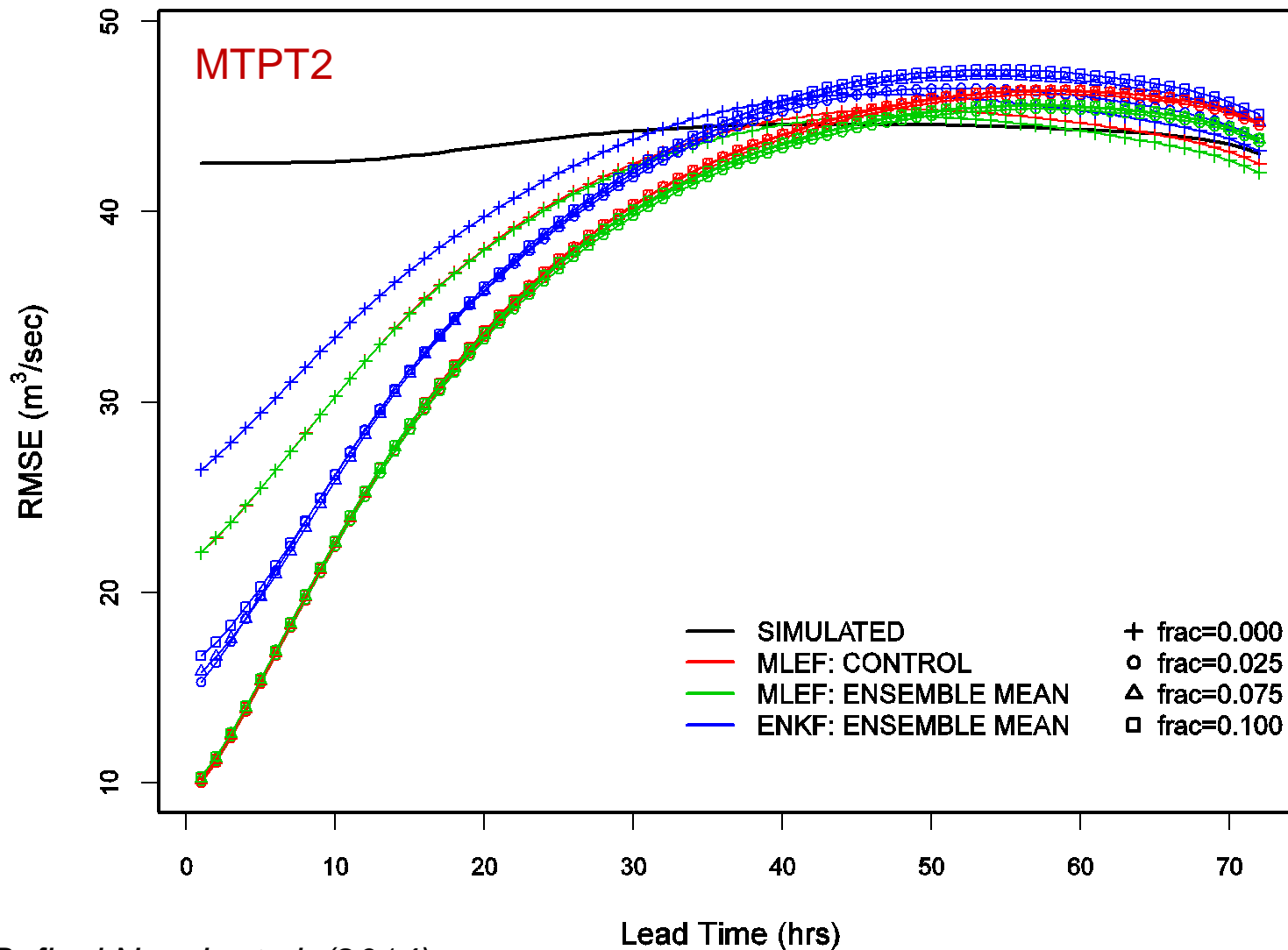
$\mathbf{w}(n)$ white system driving uncertainty, a K_1 vector

$\mathbf{x}(0)$ initial condition which may be uncertain

n time

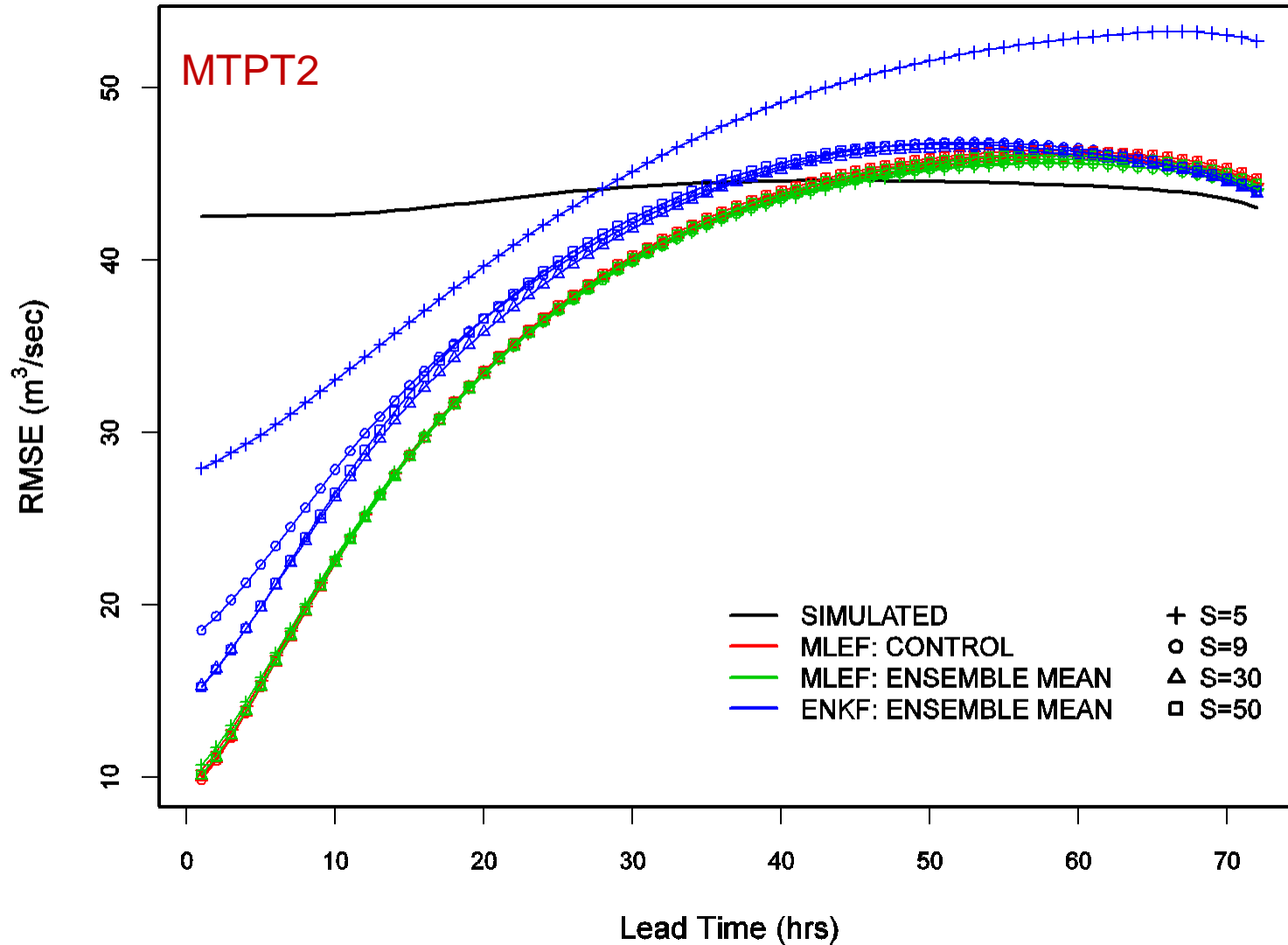
From Schweppe (1973)

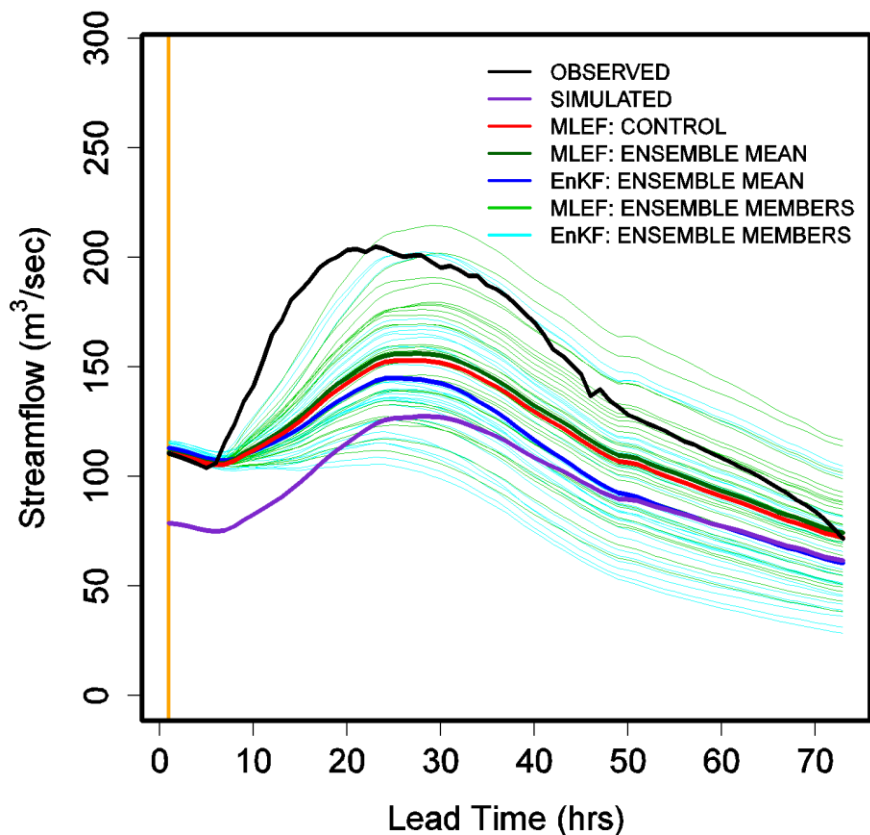
EnKF (Evensen 1994) vs. MLEF (Zupanski 2005)



From Rafieei Nasab et al. (2014)

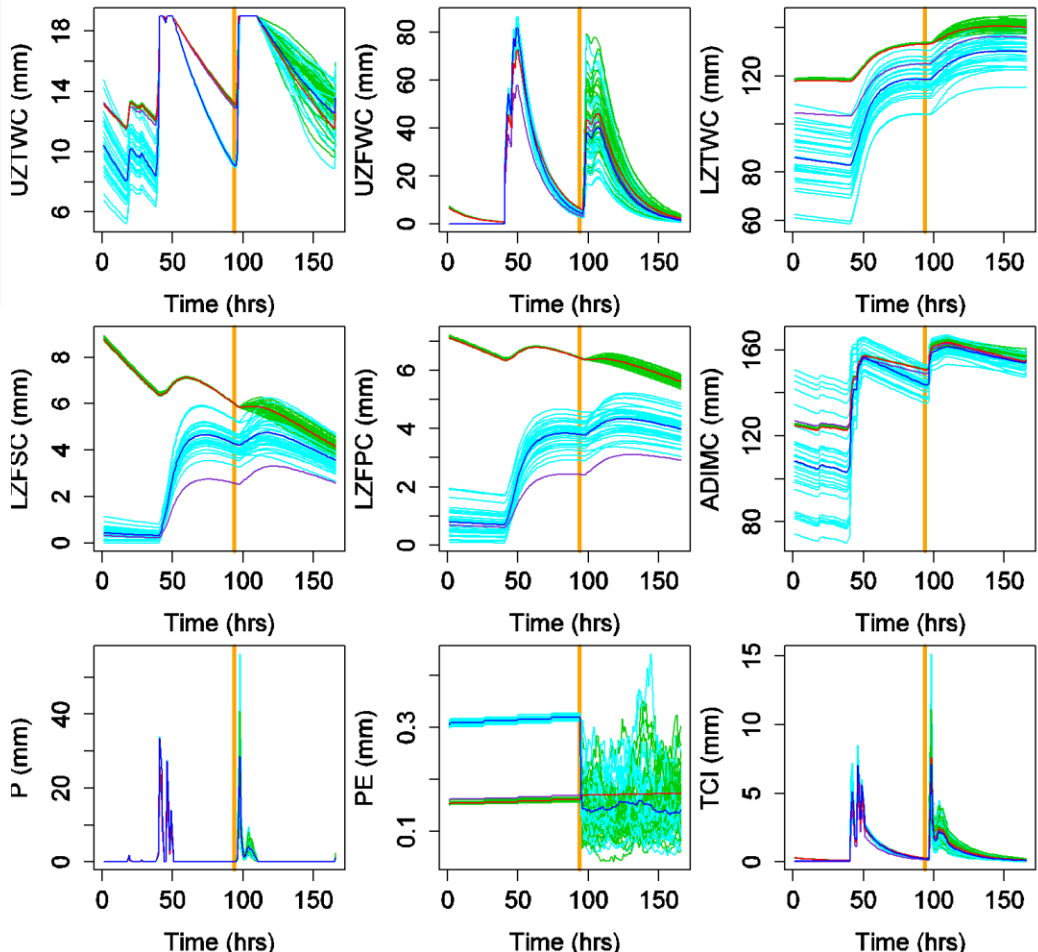
Sensitivity to ensemble size

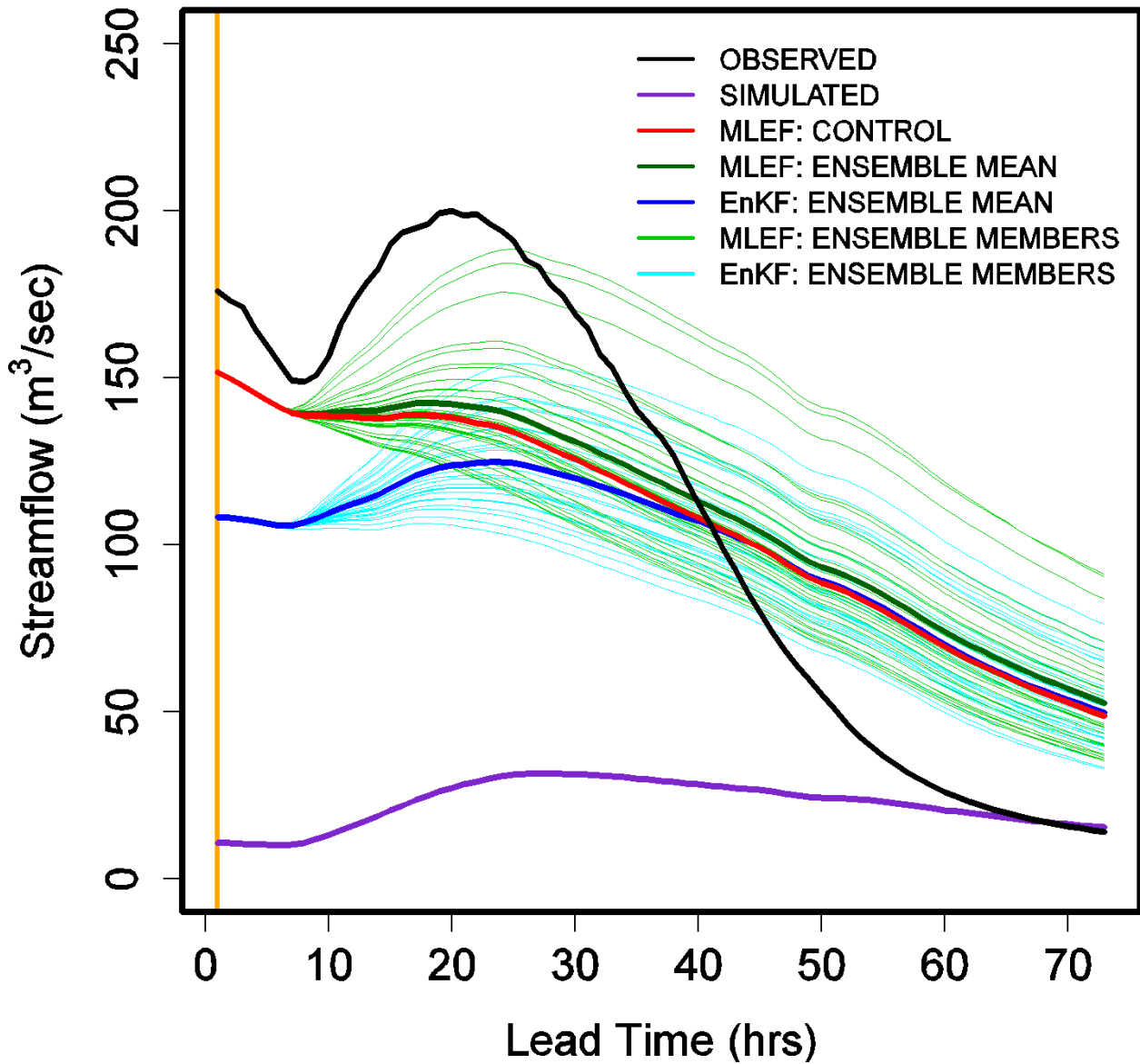




EnKF and MLEF solutions for soil moisture, however, are quite different

EnKF and MLEF streamflow ensembles are often similar





EnKF solution may be very poor.

Does minimization of mean square error suffice?

Choose the $\mathbf{x}(N)$ and $\mathbf{w}(n)$, $n = 0, \dots, N - 1$, which minimize

$$\begin{aligned} & J[\mathbf{x}(N), \mathbf{w}(0) \dots \mathbf{w}(N - 1)] \\ &= \sum_{n=0}^{N-1} [\mathbf{z}(n) - \mathbf{H}(n)\mathbf{x}(n)]' \mathbf{R}^{-1}(n) [\mathbf{z}(n) - \mathbf{H}(n)\mathbf{x}(n)] \quad (6.5.1) \\ &+ \sum_{n=0}^{N-1} \mathbf{w}'(n) \mathbf{Q}^{-1}(n) \mathbf{w}(n) + \mathbf{x}'(0) \boldsymbol{\Psi}^{-1} \mathbf{x}(0) \end{aligned}$$

subject to the constraint that

$$\mathbf{x}(n + 1) = \boldsymbol{\Phi}(n)\mathbf{x}(n) + \mathbf{G}(n)\mathbf{w}(n)$$

where $\mathbf{R}(n)$, $\mathbf{Q}(n)$, and $\boldsymbol{\Psi}$ are positive definite matrices chosen by engineering judgement.

Let $\hat{\mathbf{x}}(N|N)$ denote the resulting value of $\mathbf{x}(N)$. If one actually performs the minimization using Lagrange multipliers, the resulting equations for $\hat{\mathbf{x}}(N|N)$ are the same as those of Sections 6.2 and 6.3.

From Schweppe (1973)

Motivation for adding penalty for Type-II CB

- For accurate estimation/prediction of large amounts, reducing conditional bias (CB), in particular Type-II CB, is just as important as minimizing unconditional error variance
- Type-I CB $E[X | \hat{X}] - \hat{X}$ (analogous to reliability)
- Type-II CB $E[\hat{X} | X] - X$ (analogous to discrimination)
 - Climatological estimates are conditionally unbiased in the Type-I sense but conditionally biased in the Type-II sense
 - Perfect estimates are conditionally unbiased both in the Type-I and Type-II sense
- The focus here is on Type-II CB

Fisher solution to optimal linear estimation

$$\mathbf{z} = \mathbf{H}\mathbf{x} + \mathbf{v}$$

\mathbf{x} : completely unknown

$$E\{\mathbf{v}\} = \mathbf{0}$$

$$E\{\mathbf{v}\mathbf{v}'\} = \mathbf{R}$$

$$\Sigma = [\mathbf{H}^T \mathbf{R}^{-1} \mathbf{H}]^{-1}$$

$$\hat{\mathbf{X}} = [\mathbf{H}^T \mathbf{R}^{-1} \mathbf{H}]^{-1} \mathbf{H}^T \mathbf{R}^{-1} \mathbf{Z}$$

From Schweppe (1973)

“Fisher-like” solution for minimizing

$$J = \sum_{EV} + \alpha \sum_{CB}, \quad \alpha \geq 0$$

$$\Sigma = B[\hat{H}^T \Lambda^{-1} H]^{-1}$$

$$X^* = [\hat{H}^T \Lambda^{-1} H]^{-1} \hat{H}^T \Lambda^{-1} Z$$

where

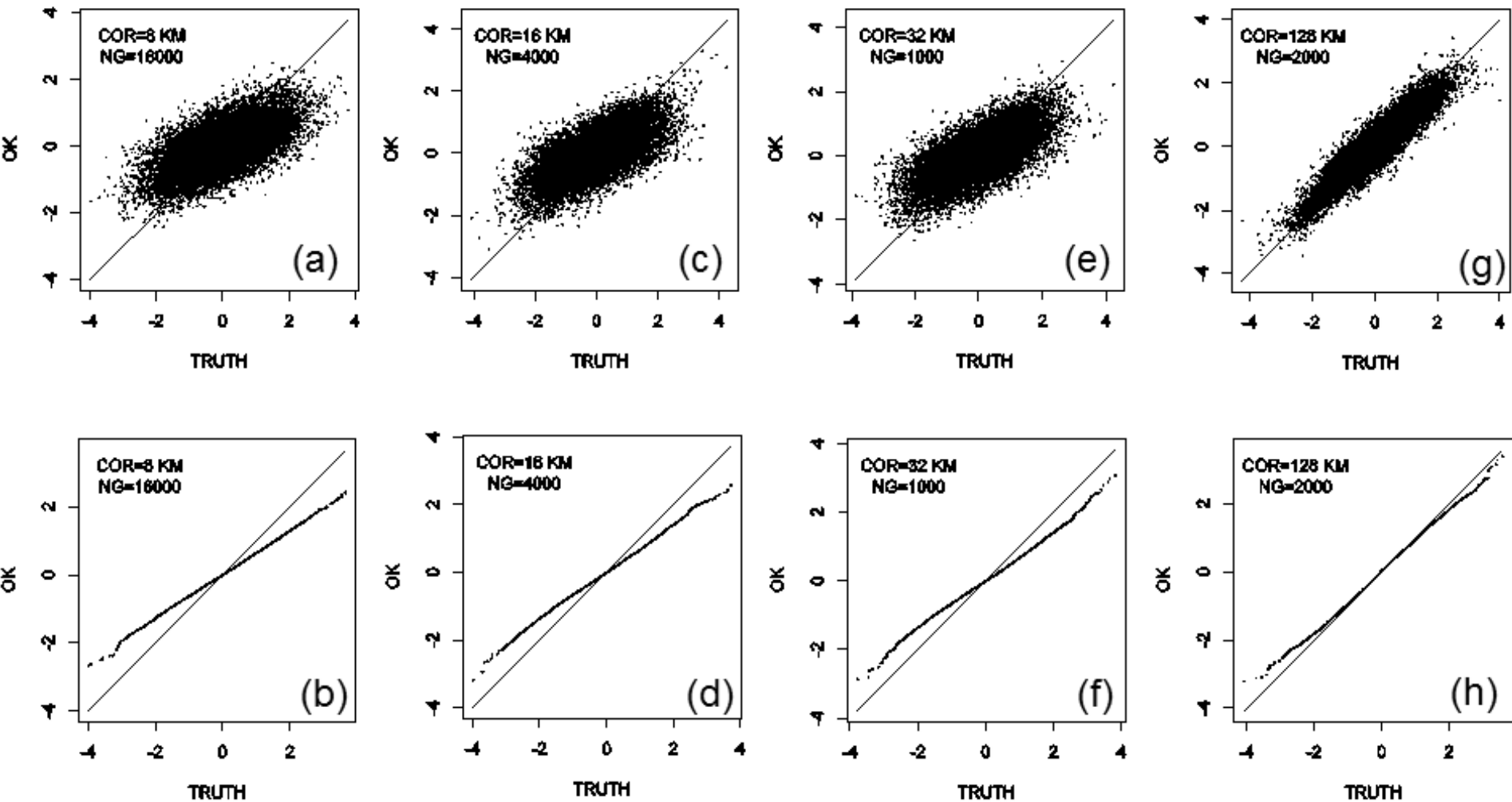
$$\hat{H}^T = H^T + \alpha \Psi_{XX}^{-1} \Psi_{XZ}$$

$$\Lambda = R + \alpha(1 - \alpha) \Psi_{ZX} \Psi_{XX}^{-1} \Psi_{XZ} - \alpha H \Psi_{XZ} - \alpha \Psi_{ZX} H^T$$

$$B = \alpha \Psi_{XX} \hat{H}^T \Lambda^{-1} \hat{H} + (1 + \alpha) I$$

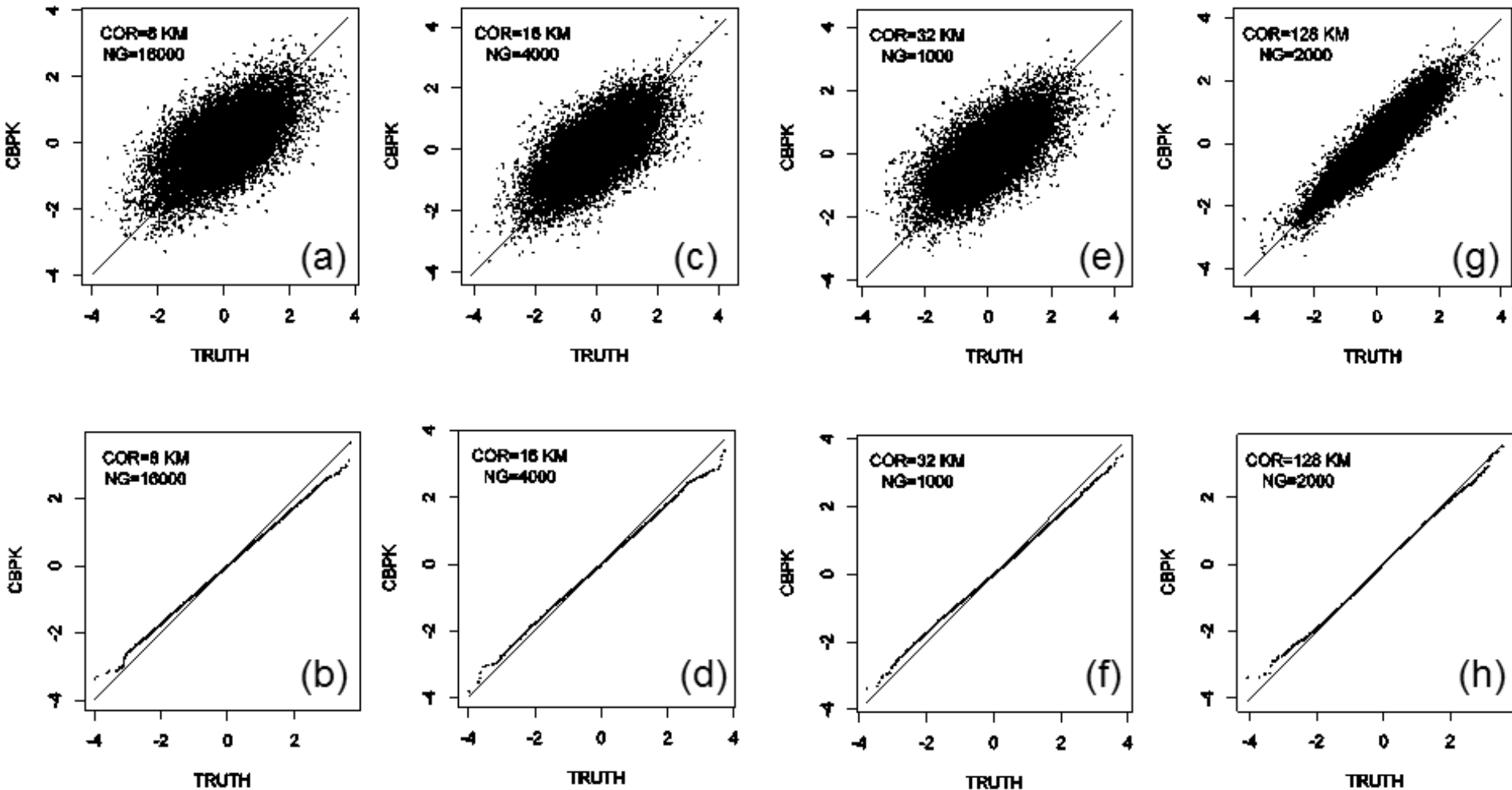
From Seo (2013), Seo et al. (2014)

OK/KF estimates vs. truth



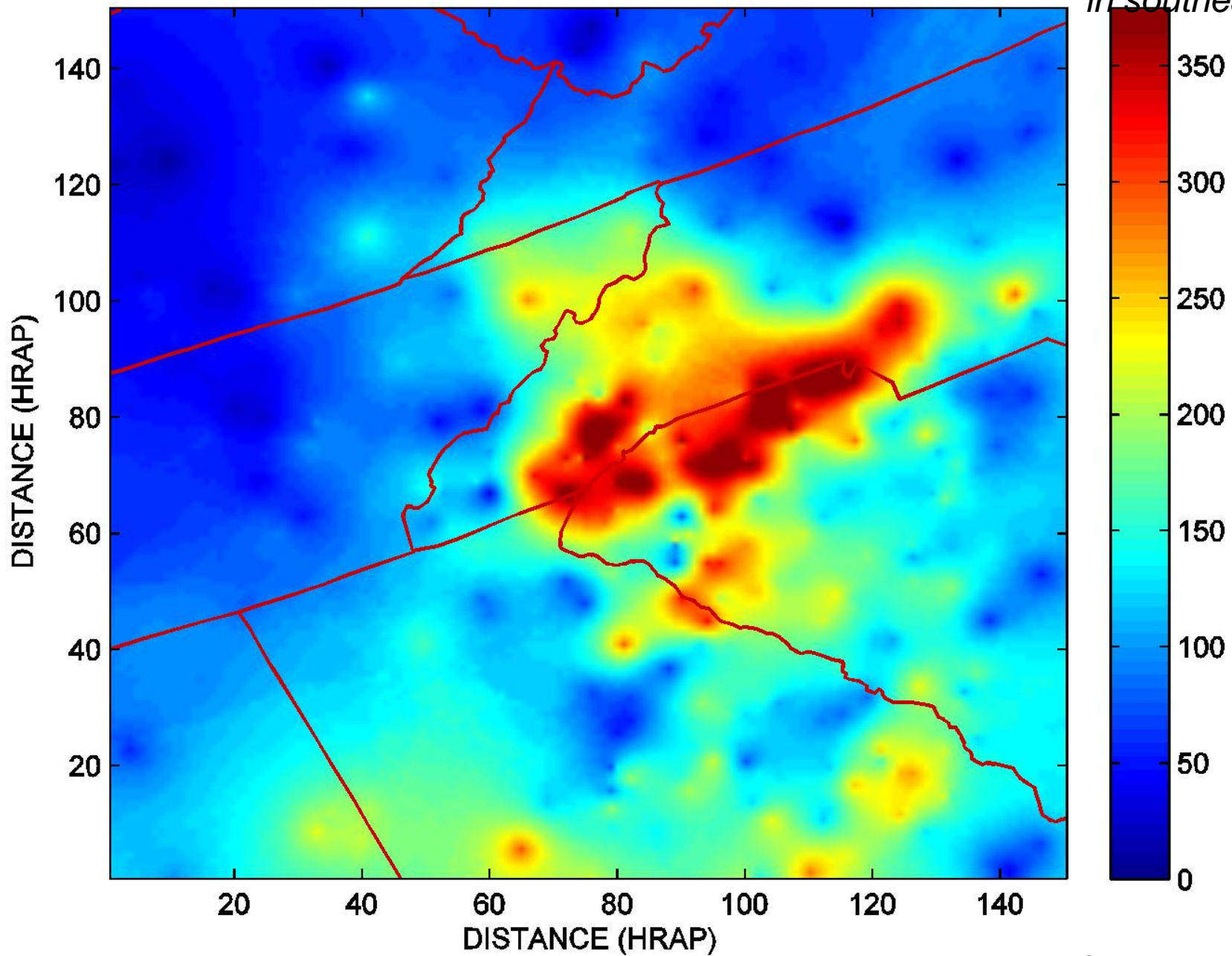
From Seo (2013)

CBPK/CBPKF estimates vs. truth



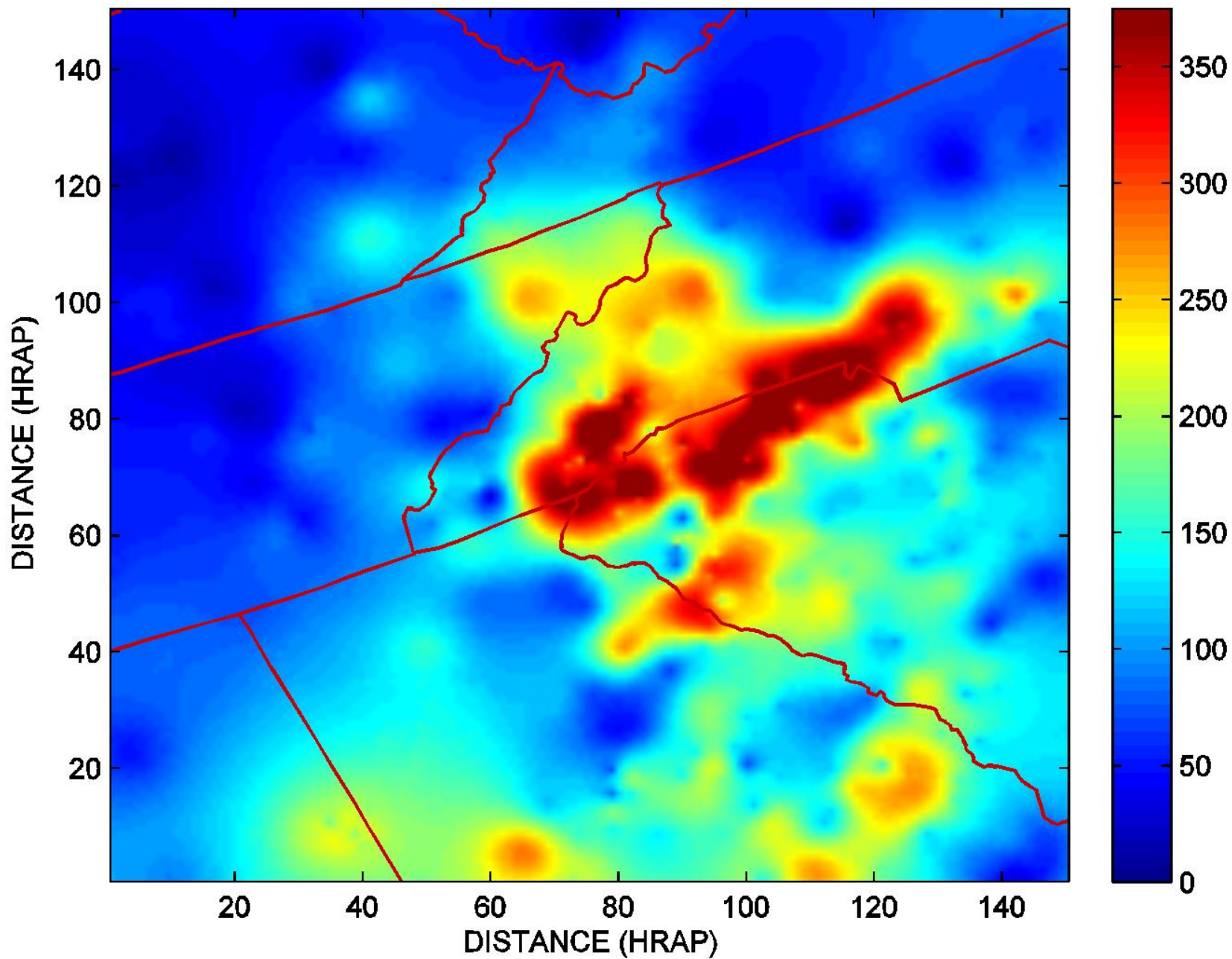
Sep 2009 Extreme Precipitation Event
in southeast US

OK (MM)

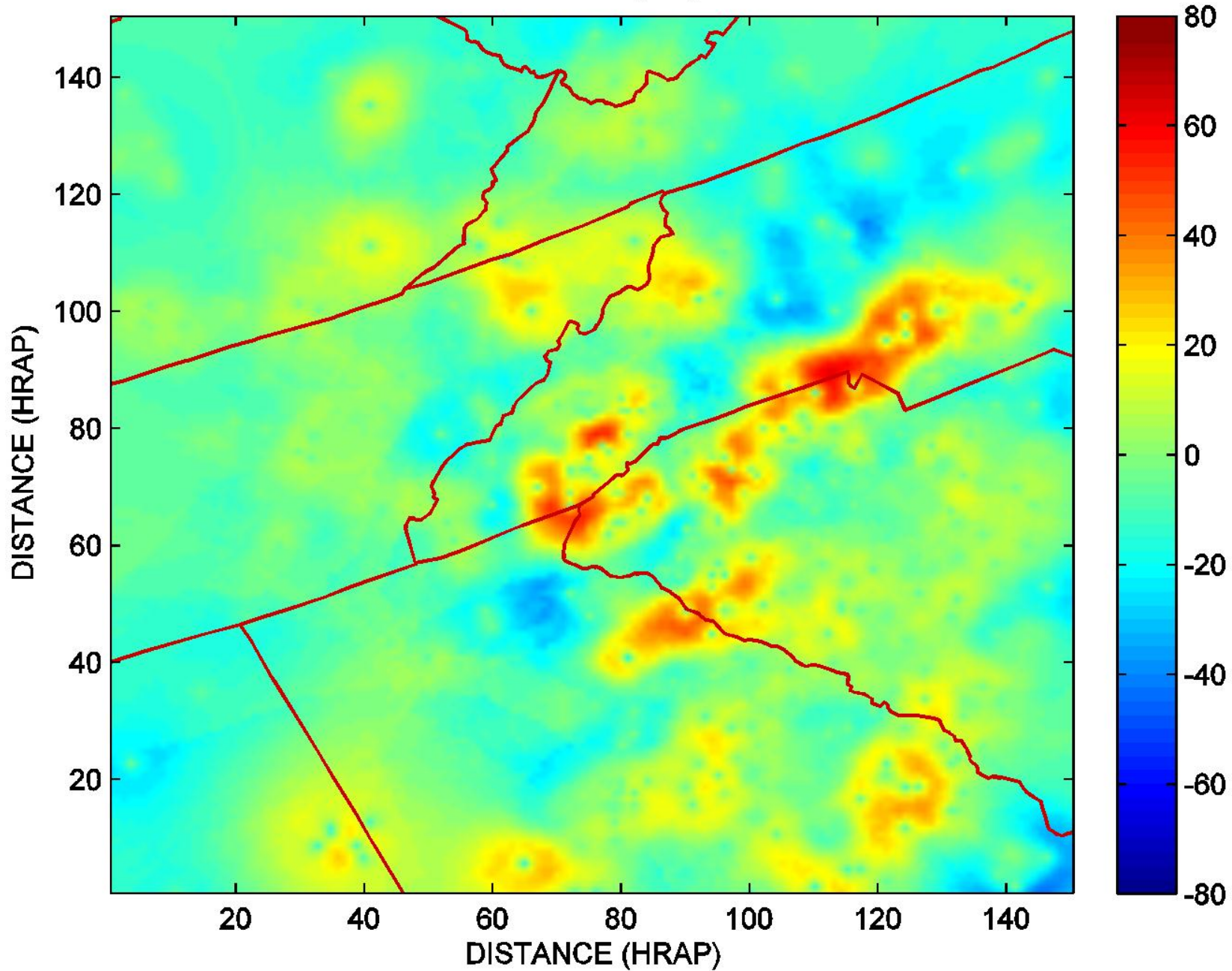


From Seo et al. (2014)

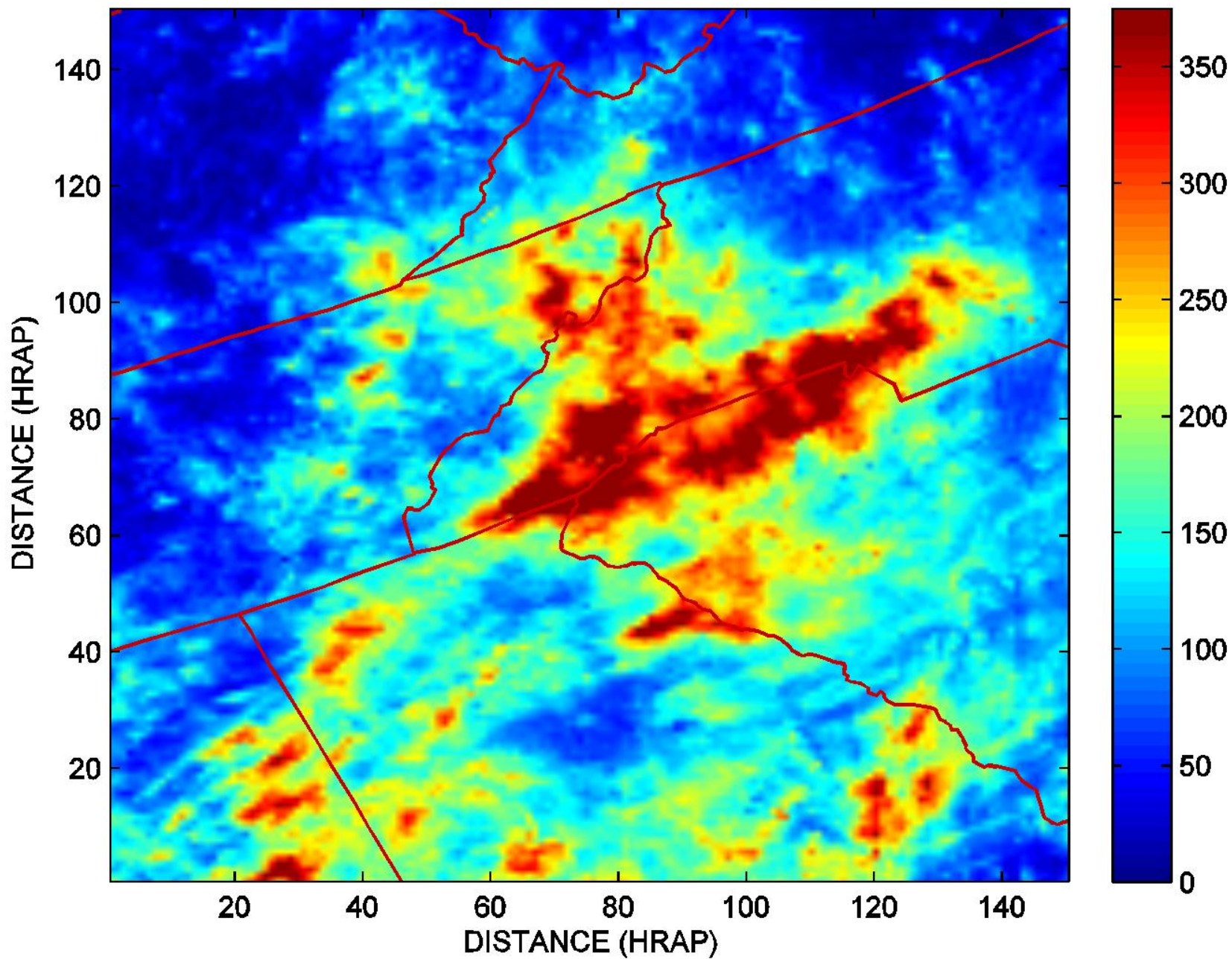
ECBPK (MM)

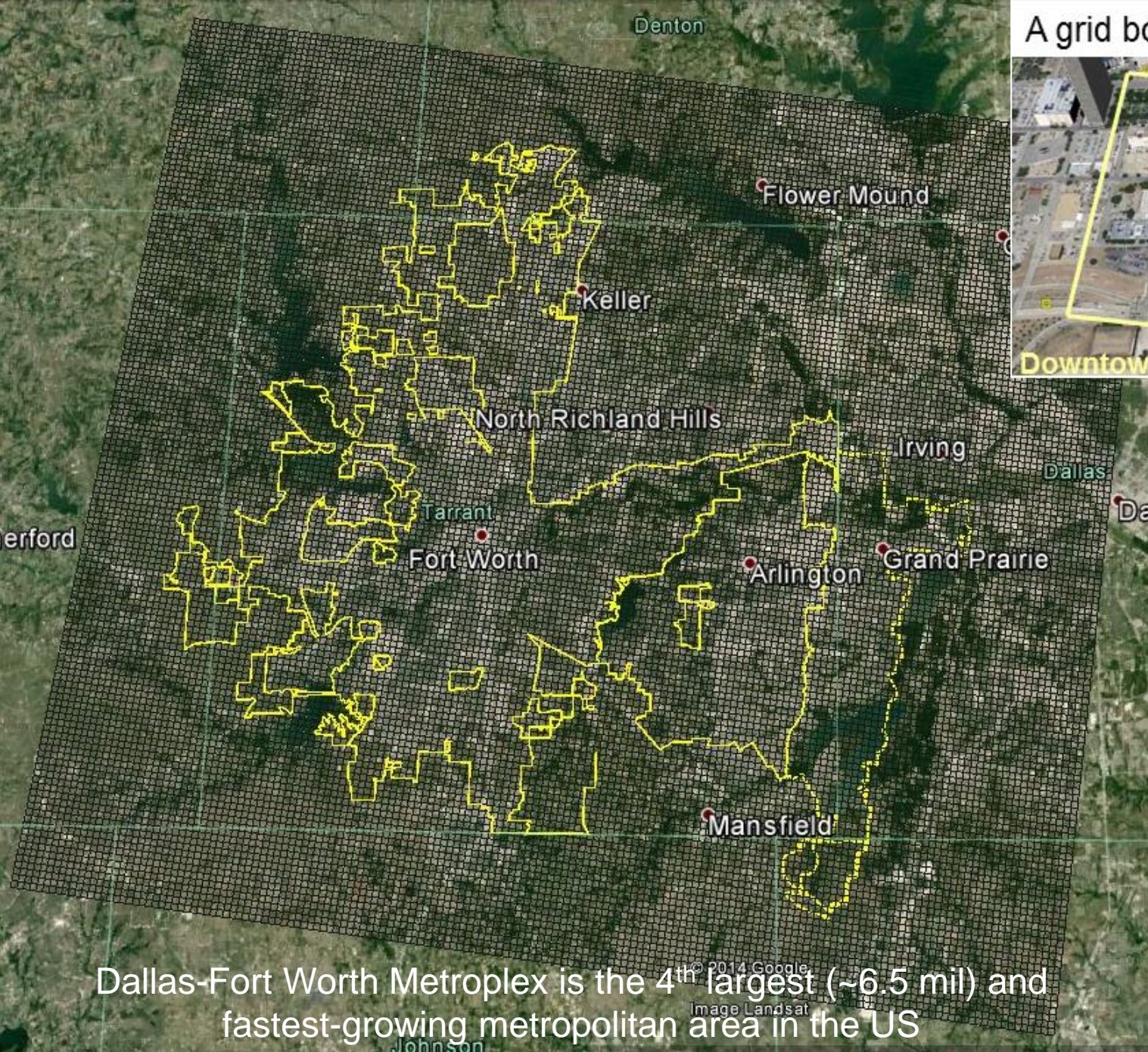


ECBPK-OK (MM)

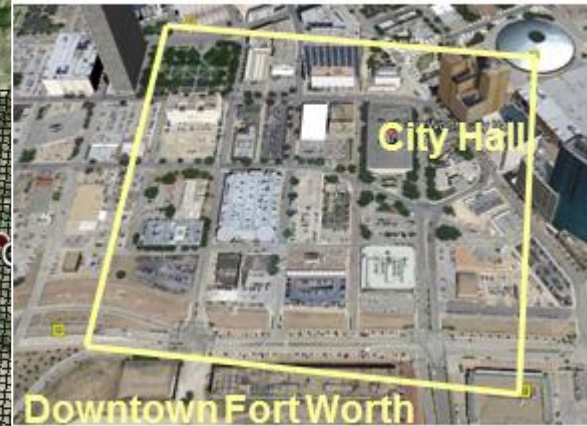


STAGE IV (MM)





A grid box (~500 x 500 m²)

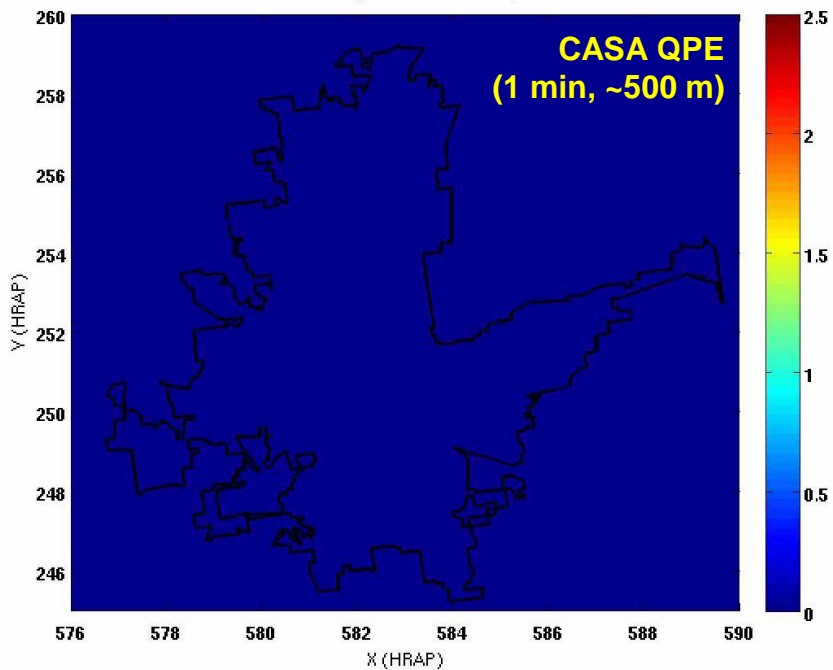


The HLRDHM domain encompassing Fort Worth, Arlington and Grand Prairie.

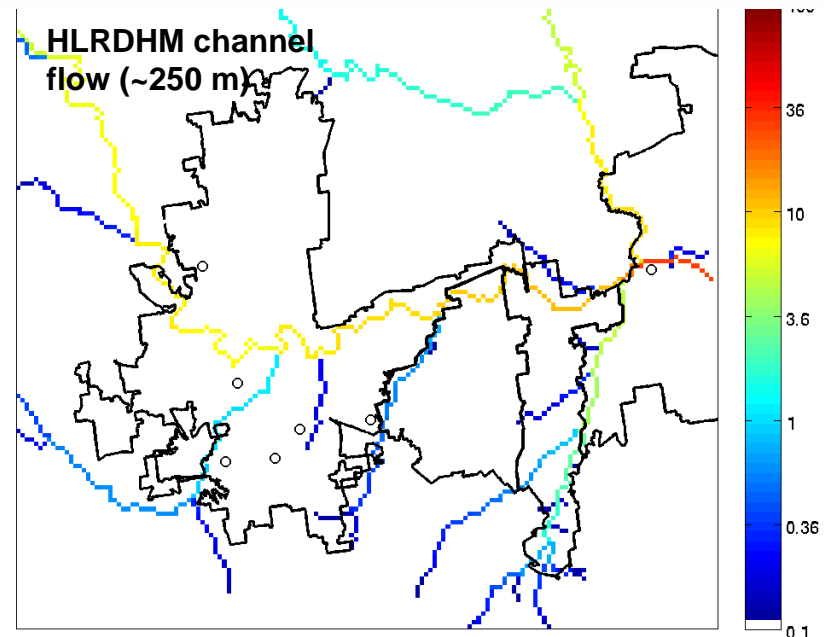
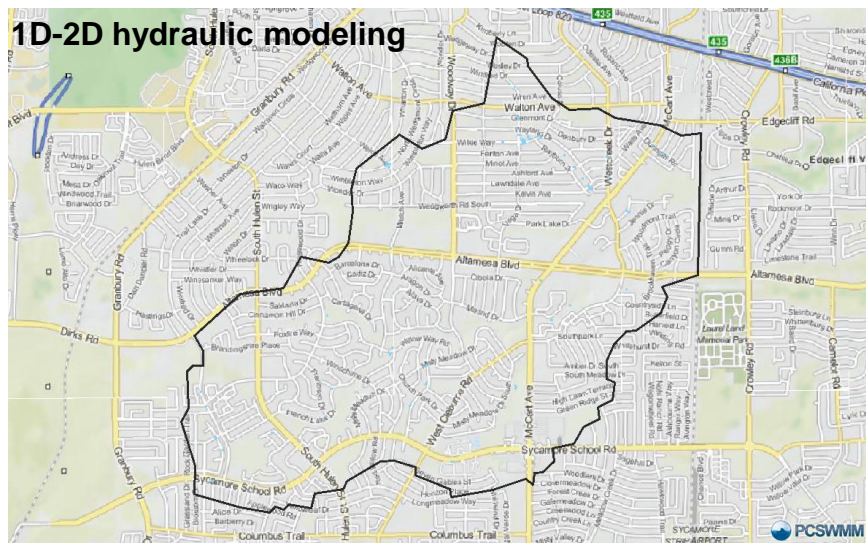
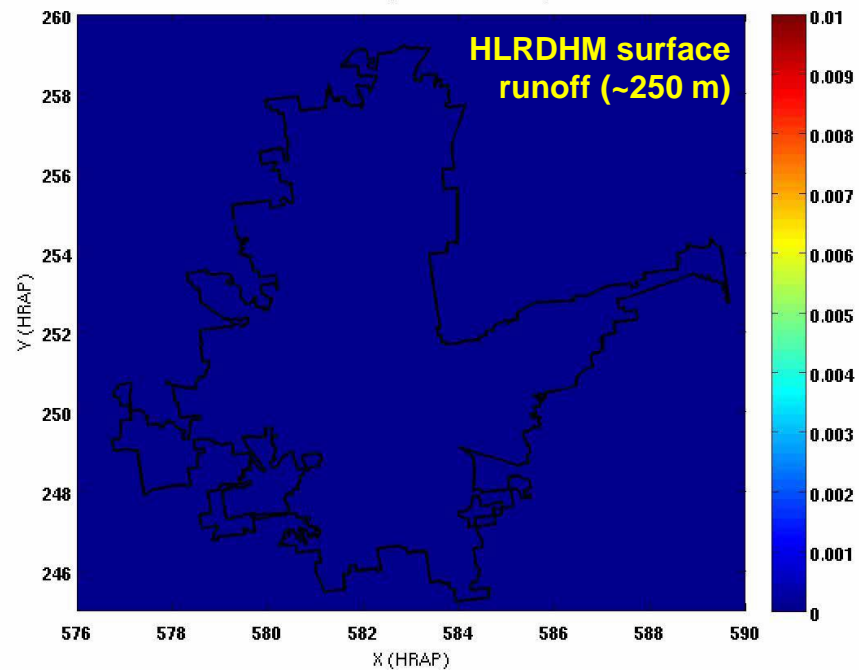
Overlaid is the 500x500 m² CASA QPE grid.

Dallas-Fort Worth Metroplex is the 4th largest (~6.5 mil) and fastest-growing metropolitan area in the US

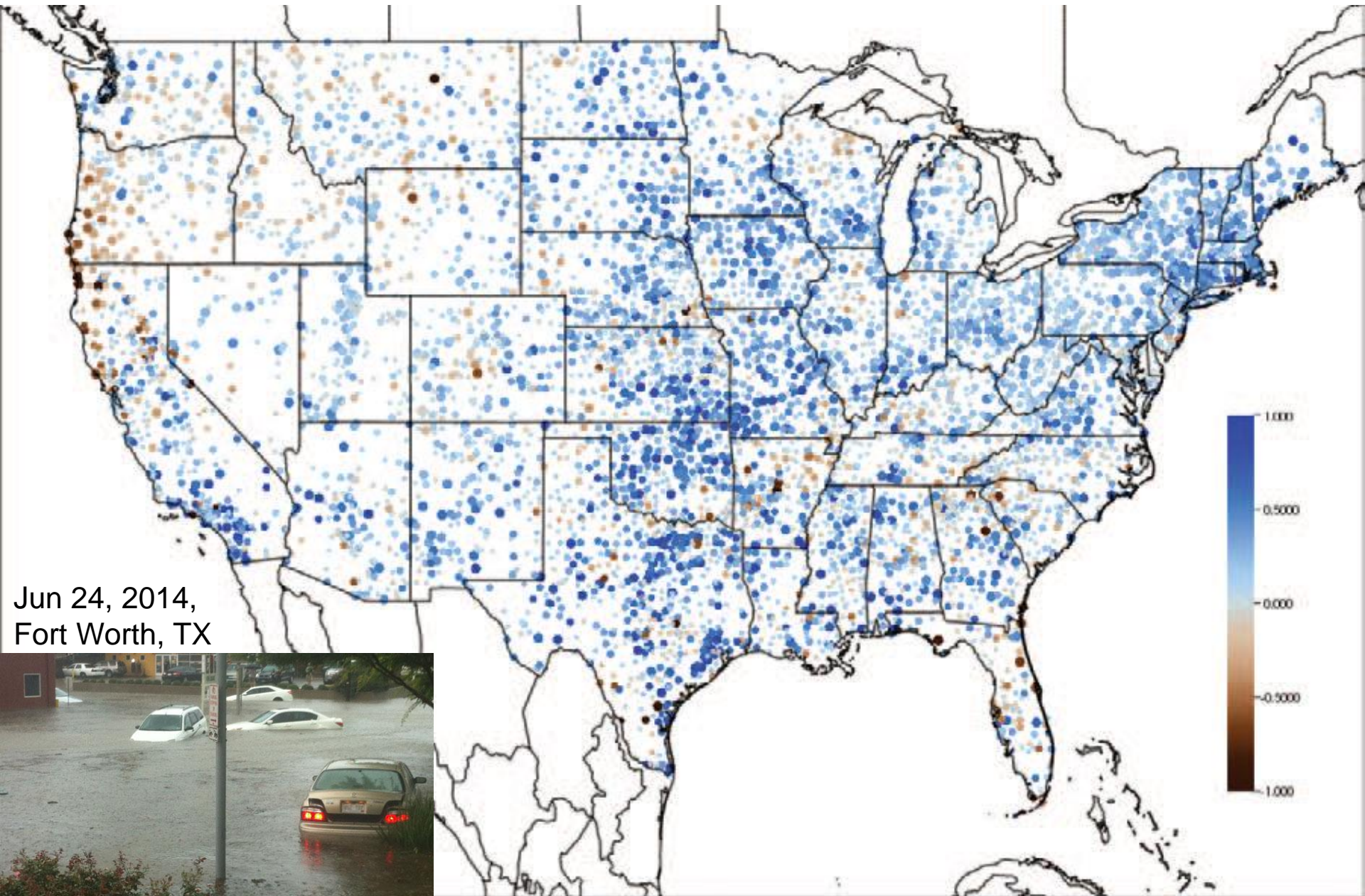
Rainrate (Jan-29-2013-20-38)



Surface Runoff (Jan-29-2013-20-38)



Changes in observed 20-yr return value of the daily accumulated precipitation (in.) from 1948 to 2010 (Kunkel et al. 2013)

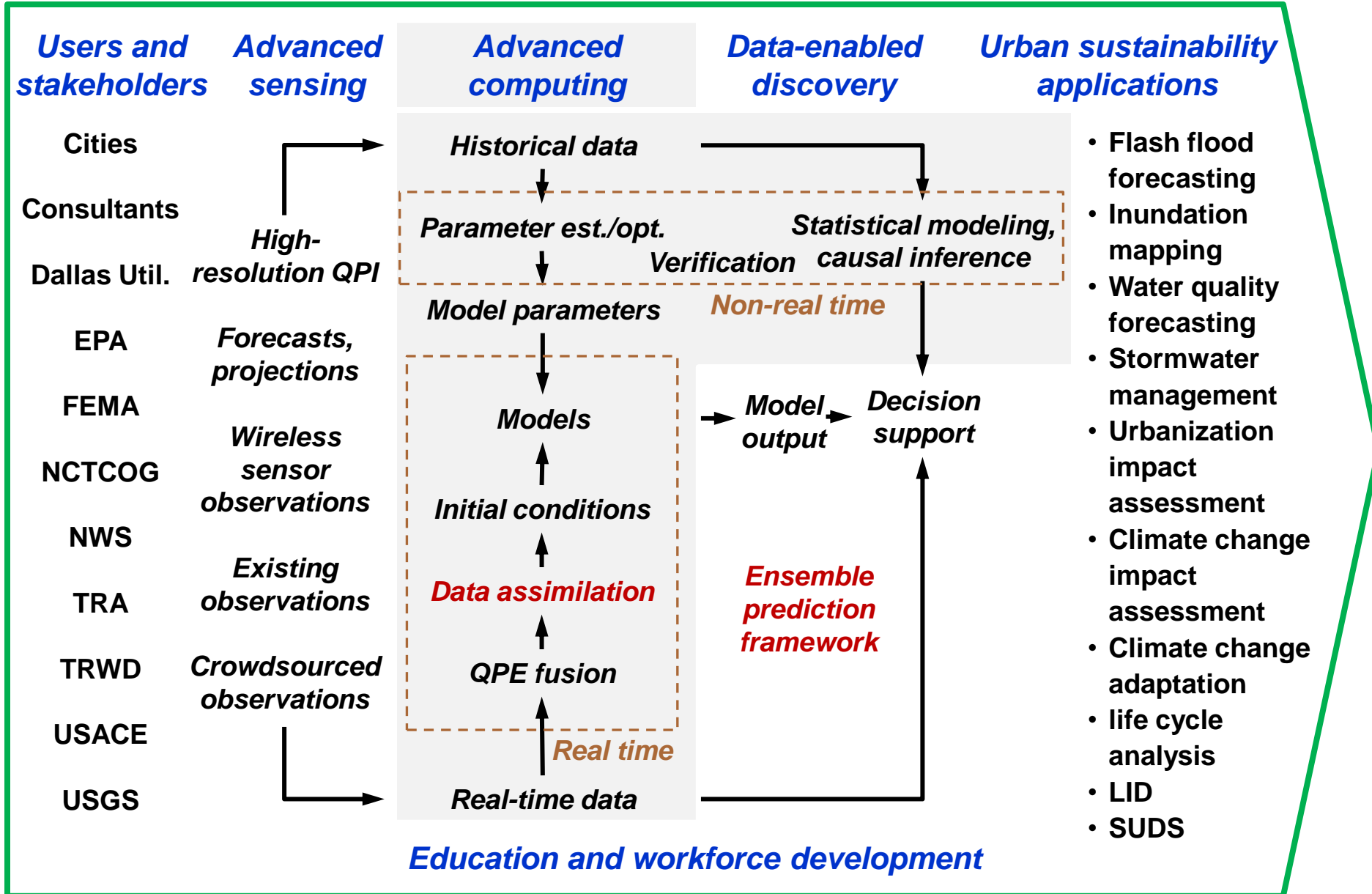


Jun 24, 2014,
Fort Worth, TX



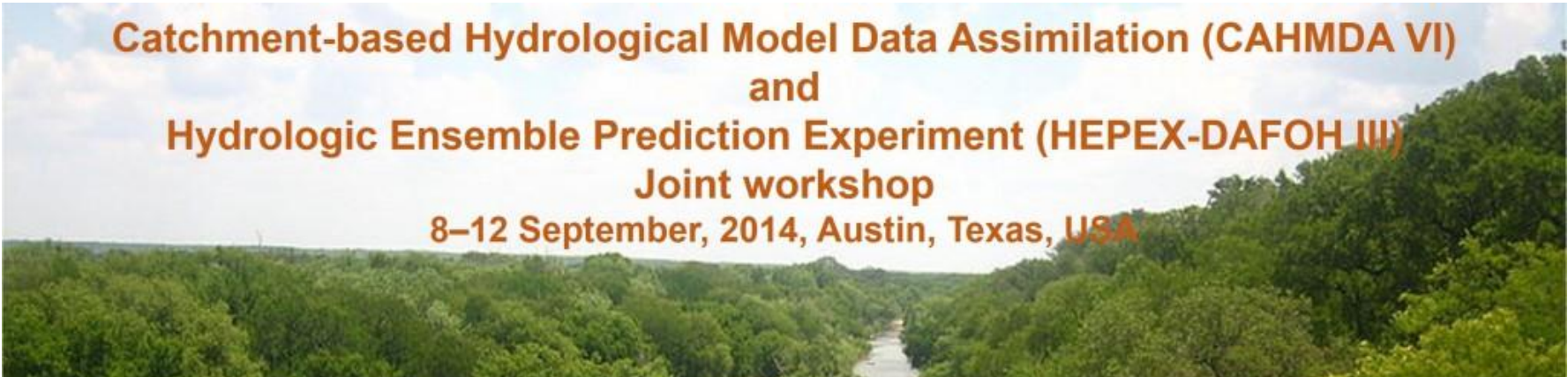
Jun 26, 2014

Ensemble prediction for urban applications – Dallas-Fort Worth Metroplex example



CAHMDA-DAFOH

<http://www.jsg.utexas.edu/ciess/cahmda-vi-hepex-dafoh-iii/>



**Catchment-based Hydrological Model Data Assimilation (CAHMDA VI)
and
Hydrologic Ensemble Prediction Experiment (HEPEX-DAFOH III)
Joint workshop
8–12 September, 2014, Austin, Texas, USA**

Abstract submission Deadline	June 30, 2014 (extended)
Early Registration Deadline	June 30, 2014
Training Course	Sep 06-07, 2014
Joint CAHMDA-VI and HEPEX-DAFOH III Workshop	Sep 08-12, 2014
Excursions and Activities	Sep 13, 2014



THANK YOU

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